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THE DRAG OF AIRSHIPS

DRAG OF BARE HULLS - II

By Lieut. Clinton H. Havill, U.S.N.

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## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS.

## TECHNICAL NOTE NO. 248.

## THE DRAG OF AIRSHIPS.

## DRAG OF BARE HULLS - II.

By Clinton H. Havill.

## Summary

The extension of wind tunnel tests of models of airship hulls to full scale requires an extension from a  $VL$  of the order of less than 500 sq.ft./sec., to the order of 80000 sq.ft./sec., where  $V$  = air speed, feet per second,  $L$  = length in feet of the particular form of hull. The reason for this research was to furnish the airship designer with a method for finding the  $VL$  curve of any conventional type of hull, using data obtained from actual performance of airships flown prior to 1926.

This digest as given here in Part II, was begun in preliminary details, in June, 1922, and completed in April, 1926, as it was necessary to complete Part I before Part II could be completed; the period between September, 1923, and December, 1925, was devoted to work on Part I.

The outstanding results are as follows:

1. An empirical method for finding the drag coefficient of any bare airship hull with its  $VL$  curve from 100,000 cu.ft. volume to 6,400,000 cu.ft. volume. (See diagrams Figs. 7 and 8)

and example to illustrate its use.)

2. The derivation of an empirical shape coefficient that can be calculated from the hull contour that defines the VL curve of any conventional airship shape within the limits placed on Figs. 7 and 8.

3. (a) That the slope of each VL curve differs with each type of hull and that its slope is not quite constant.

(b) That  $C_H = \text{function of } (VL)^n$  and  $n$  is a variable at different values of VL.  $C_H$  = drag coefficient of bare airship hull. Drag =  $C_H \frac{0}{2} (\text{Volume})^{2/3} V^2$ .

(c) That the value of  $n$  varies slowly so that extrapolations beyond that given by diagrams Figs. 7 and 8. of the VL curve are not much in error, as requirement 3 of illustrative problem shows.

4. The region from model tests to a volume of 100,000 cu.ft. size indicates that in this region the most rapid change in the slope occurs with the conclusion that "The best model in the wind tunnel will probably be the best (lowest drag) airship hull but not necessarily" as their VL curves may cross and again may re-cross at higher values of VL. In view of this as found by extrapolating the VL curves calibrated on performance back to wind tunnel values and extrapolating wind tunnel results to higher values of VL together with the fact that airship designers are not interested in airship hulls of less than

100,000 cu.ft. of volume, this part of these researches was left out. The scale on diagrams at .3 cu.ft. volume calibrated on existing wind tunnel data is merely for general information.

### Introduction

The principal components of the drag of bodies in a wind stream has been laid down by Reynolds, Stanton, Munk, Prandtl, Froude, Bairstow and others, so that it is not necessary to outline their work here. Reference to the summary of their work in the recent N.A.C.A. Technical Report No. 219, "Some Aspects of the Comparison of Model and Full Scale Tests" by D. W. Taylor, is invited, which expressed in words: Drag = pressure difference + skin friction + wave making + compressibility effect.

$$\text{Symbols Drag} = R = \text{Drag} = F_1 (\rho L^2 V^2) F_2 \left( \frac{\rho VL}{\mu} \right) F_3 \left( \frac{Lg}{V^2} \right) F_4 \left( \frac{V^2}{V_s^2} \right)$$

L = Linear dimensions of length.

V = Air speed.

$\rho$  = Mass density of air.

$\mu$  = Viscosity.

$V_s$  = Velocity of sound in air.

G = Acceleration of gravity.

R = Drag.

It has been well established in theory and practice that as far as airships are concerned the compressibility effect expressed by  $\left( \frac{V^2}{V_s^2} \right)$  is negligible or zero as the air speeds in flight are

so far below the speed of sound at which compressibility exists. The wave making ( $\frac{L^2}{V^2}$ ) so important in surface ships is negligible in airships and if it does exist in a microscopic percentage, can be included in the constants and exponents in the remaining two. So that  $R = F_1 (\rho L^2 V^2) F_2 \left(\frac{\rho VL}{\mu}\right)^n$  where  $n$  is a variable depending on type of hull - fineness ratio, virtual volume, length, diameter, eccentricity of nose ellipse, cylindrical coefficient, and on the value of  $VL$  as found out in this research. Or, if reduced to a standard value of kinematic viscosity of  $\frac{\rho}{\mu}$  then  $R = \text{constant } (\rho L^2 V^2) F_2 (VL)^n$ .

Let  $3K = \text{the constant; } (\text{Volume})^{2/3} = L^2$ ,

then  $R = K \frac{\rho}{2} (\text{Volume})^{2/3} V^2, F_2 (VL)^n$ .

Let  $C_H = K + \frac{F_2 (VL)^n}{\frac{\rho}{2} (\text{Volume})^{2/3} V^2}$ ,

then  $R = C_H \frac{\rho}{2} (\text{Volume})^{2/3} V^2$  in which case it is seen that  $C_H$  is a variable depending on the value of  $(VL)^n$ .

It now remains to give a method of finding the value of  $C_H$  knowing the contour and size of the airship hull. In brief, this was done by taking the whole ship performance of a large number of ships (all Zeppelin types and Navy nonrigids) as given in Part I, and calculating their external drag and getting the hull drag. Then to find a quantity of linear dimensions that is calculated from the contour and size of each ship such that

if the drag is plotted against this  $VL$  that the results show it to be a smooth curve. With this as a basis, it now was necessary to find a dimensionless quantity that would define each ship - such a quantity called here "whole hull shape coefficient" ( $Y + Z$ ) such that it could be calibrated against the various values of  $C_H$  based on performance.

#### Body of Report

An exhaustive research was made to find a dimensionless quantity that sufficiently defines a given hull and to express the relation between  $C_H$  at various values of  $VL$  and this quantity. The effective velocity over the skin of different types of hulls at different speeds was found to be so different that it could not be expressed as a constant times air speed, so the surface area times  $KV^2$  was given up as  $n$  apparently was a very sensitive quantity. So shapes were geometrically expanded to the volume of known ships for comparison. From this comparison, relative drag coefficients were obtained by discovering that the drag of an airship hull follows very closely the  $VL$  principle over a short range and results are comparable if  $L$  is defined as  $L_g$  defined here as geometric length where

$$L_g = \sqrt[4]{(\text{Volume}) + \frac{\pi r^3}{3} (\text{length})} = \sqrt[4]{(\text{Virtual Vol.}) (\text{length})};$$

this was discovered by trial and error in analyzing the wind tun-

nel results and plotting their drag in pounds versus  $VL_g$  as shown in Fig. 6.

The external drags of all the items (about 90 hulls - 26 separate types) of Part I can be separated by calculating the external drags of about six types of hulls and by simultaneous equations solving for the external drags of all the remaining types of hulls. However, the results are no better than the correctness of the external drag of the five or six types calculated. Yet these results when plotted against  $VL_g$  show a smooth curve. For this report it was better, therefore, to calculate the external drag for all the 26 types of hulls (given in Part I) and to plot them against  $VL_g$  (Fig. 1) is such a curve.

There is another way in which the external drag of various airships can be calculated, and that is to assume that the percentage of external drag remains the same part of the total as wind tunnel experiments indicate. In general, wind tunnel results show nonrigid types to have about 60% total drag = external drag; and rigid Zeppelin types to have 40% total drag = external drag. The exact percentage will of course vary with the type of cars, fins, struts, wires, etc., but various percentages can be assumed on each type based entirely on engineering judgment. The remaining hull drags, if plotted against  $VL_g$ , will give Fig. 2.

Now the mean between Fig. 1 and Fig. 2, is Fig. 3. In view of the fact that Fig. 1 and Fig. 2 give a curve that is practi-

cally identical, it gives in Fig. 3 a basis of comparison of hull drag coefficients when ships are expanded or contracted to the same volume and the same speed. In other words, the ratio of hull drag coefficients ( $C_H$ ) at the same volume and speed is the ratio of the drags of the bare hulls as

$$\frac{\text{Drag of hull 1}}{\text{Drag of hull 2}} = \frac{C_{H1} \frac{\rho}{2} (\text{Vol})^{2/3} V^2}{C_{H2} \frac{\rho}{2} (\text{Vol})^{2/3} V^2};$$

if  $\rho$ , (Vol), and  $V$  are the same for both ships, then

$$\frac{\text{Drag of hull 1}}{\text{Drag of hull 2}} = \frac{C_{H1}}{C_{H2}}.$$

Now with curve [drags, vs.  $(VL_g)$ ] as in Fig. 3, the comparison of ships at different volumes and  $V = 100$  ft./sec., can be carried out. A comparison at 100,000; 200,000; 400,000; 800,000; 6,400,000 was carried out. It necessitated a small extrapolation of curve (Fig. 3) to get 6,400,000 yet as the curve is fairly definite and the value of  $(\frac{\rho}{\mu} VL_g)^n$  shows  $n$  to change value so slowly that this extrapolation is justified.

From here on various methods were tried to find a dimensionless quantity which would show to be a function of these values of  $C_H$  that comparison indicated. If such a quantity was established it could be represented on a plot or diagram and calibrated on the comparative results.

Speed and density was kept constant so that for a given volume the relative values of  $C_H$  were the same as the relative

values of their drags as  $\frac{\rho}{2} (\text{Vol})^{2/3} V^2 = \text{constant}$ . The dimensionless quantity that proved to sufficiently define a hull and to have no conflicts with the comparative results was  $(Y + Z)$ .  $Y = (\text{eccentricity of nose ellipse}) (\text{cylindrical coefficient})$  (fineness ratio);  $Z = \left( \frac{\text{length}}{\text{geometric length}} \right)$  (fineness ratio).

Hulls were now grouped according to their values of  $Y$  and the parametric equation of  $Y$  against  $C_H$  was plotted (Fig. 4) where  $C_H$  was the total hull drag coefficient of ships with the same value of  $Y$ . A mean curve was drawn through the points plotted - a curve for volumes 100,000; 800,000; 6,400,000 cu.ft. Likewise, for  $Z$  on Fig. 5. It is to be noted that  $Y = (e) \left( \frac{4 \text{ Vol}}{\pi D^2 L} \right) \times \left( \frac{L}{D} \right) = (c) \left( \frac{4 \text{ Vol}}{\pi D^3} \right)$ , is independent of length except as length affects volume. An interesting research by simultaneous equations by the author reveals that this function  $Y$ , for the ten ships on which it was calculated, appears to be a true function of that part of the drag due to pressure difference, and that  $KYL^2V^2 + F_2 Z \left( \frac{\rho VL}{\mu} \right)^n = R$  gives  $K$  a constant for all values of  $VL$ . The writer hopes to be able to analyze all existing ships, in the near future, in order to prove or disprove this relation. Rather letting Fig. 4 indicate  $C_H = F_1 Y + F_2 Z$  and plot total  $C_H$  against  $Y$  and likewise  $Z$  in Fig. 5. This amounts to a calibration of  $Y$  and  $Z$  on  $C_H$ .  $Z = \frac{L}{L_g D} \times \frac{L}{D} = \frac{L^2}{L_g D}$  gives length the predominate factor

effect in Z. Now with the values of Y and Z for each model in the wind tunnel the values of  $C_H$  according to Y called  $C_{HY}$  and the values of  $C_H$  called  $C_{HZ}$  according to Z were picked off. To let each have its proper effect, the formula

$$\frac{Y C_{HY} + Z C_{HZ}}{Y + Z} = C_H \text{ for given } (Y + Z) \text{ was used to give the value of } C_H \text{ at the various volumes. With these various values of } C_H \text{ from model to full scale on the 17 models, the scales could be calibrated.}$$

The interval from .3 cu.ft. volume to 100,000 cu.ft. volume was calibrated on the diagrams (Figs. 7 and 8) and the slope given. The remaining ships from Part I were now added to give a complete calibration at 100,000; 800,000; and 6,400,000 cu.ft. volume; (An exploration of the region just beyond the usual wind tunnel model size (100 cu.ft. volume) indicates that perhaps some very sharp changes in VL curve is probable) so that the slope lines from .3 cu.ft. to 100,000 cu.ft. are the mean over this part of the VL curve. However, beyond 100,000 cu.ft. volume the diagrams in Figs. 7 and 8 will give the VL curve very accurately if used in the manner as shown by the example (Fig. 9). Since the scales are not uniform sight interpolation of values of  $C_H$  at various volumes other than 100,000; 800,000; and 6,400,000 are very misleading. The illustrative problem shows how to get the value of  $C_H$  (from the VL curve obtained) for other volumes.

The limits from which this data is designed are placed on each diagram and there is no justification for using it other than within the limits given: However, these limits will cover practically all contours of airship hulls that exist or are proposed today.

Further ground for research is to separate bare hull drag into pressure difference and skin friction, a large part of which has been done during the trial and error methods used to discover the quantities Y and Z.

#### Assumptions

1. That external drag, cars, fins, wires, etc., vary as the square of the speed.
2. The coefficients used in calculating drag of cars, fins, etc., were assumed based on engineering judgment. The idea was to get the curve drag versus  $(VL_g)$  oriented at the proper order of magnitude as a further check on the results which would be obtained by the percentage of external drag method. However, it is believed that the coefficients used to calculate drag of cars, fins, wires, etc., are as nearly correct as the present science of aerodynamics can give.

Units used throughout this report are ft., lb., sec.  
Everything in this report is reduced to:

A standard density of  $\rho = .00237$  slugs/cu.ft.

A standard viscosity of  $\mu = .0000003779$  slugs/ft.sec.

A standard kinematic viscosity of  $\nu = \frac{\mu}{\rho} = .000159$  sq.ft./sec.

## Example to Illustrate Method for Use of Diagrams, Figs. 7 &amp; 8.

## Part II.

Problem:

An Airship hull is constructed with a contour like the U.S.S. Los Angeles if 100 ft. parallel section had been added at the point of maximum ordinate; and to make it such dimensions that the air volume of hull = 5,000,000 cu.ft.

## Required:

1. Hull drag coefficient- $V_s - VL$ , curve of this airship hull
2. Bare hull drag in lb. at 100 ft./sec., standard density,  
( $\rho = .00237$  slugs/cu.ft.)
3. Horsepower absorbed in overcoming bare hull drag at 120  
ft./sec.

## Data

Present dimensions of U.S.S. Los Angeles.

		Symbol
Air volume of hull	2,764,461.0	cu.ft. (Vol)
Length	653.3	ft. L
Maximum diameter	90.7	ft. D
Cylindrical coefficient	.650	$\left(\frac{4(Vol)}{\pi D^2 L}\right)$
Eccentricity of nose ellipse	.978	$\left(\frac{\sqrt{x^2 - r^2}}{x}\right) = e$
Fineness ratio	7.25	L/D

Calculations of dimensions of hull in problem and dimensionless quantities of shape.

$$(Vol) \text{ added in parallel section} \quad 100 \pi r^2 = 100 \pi 45.35^2 = 646,108 \text{ cu.ft.}$$

$$\text{Former (Vol)} \quad \frac{2,764,461}{3,410,569}$$

$$\text{New length} = L + 100 = 653.3 + 100 = 753.3 \text{ ft.}$$

$$\text{Max. diameter, as formerly} \quad 90.7 \text{ ft.}$$

$$e = \frac{.978}{\sqrt{753.3^2 - 90.7^2}} = .978$$

$$\text{New fineness ratio} \quad \frac{L}{D} = \frac{753.3}{90.7} = 8.36$$

$$\text{Cylindrical coef.} = \frac{(Vol)}{\text{Vol of circumscribing cylinder}} = \frac{4(Vol)}{\pi D^2 L} = \frac{4 \times 3,410,569}{\pi (90.7)^2 \times 753.3} = \frac{13,642,276}{19,597,764} = .6961$$

$$\text{Virtual (Vol)} = V_M (\text{Vol}) + \frac{\pi r^3}{3} = 3,410,569 + \frac{\pi (45.35)^3}{3} = 3,410,569 + 97,670 = 3,508,239 \text{ cu.ft.}$$

$$\log_{10} V_M = 6.54509$$

$$\log_{10} L = 2.87984$$

$$" (V_M L) = 9.42493$$

$$\begin{aligned} L_g &= \text{Geometric length} = \\ &= \sqrt[4]{(\text{Vol} + \frac{\pi r^3}{3}) (\text{length})} = \\ &= \sqrt[4]{V_M L} = 227.1 \text{ ft.} \end{aligned}$$

$$\begin{aligned} " \sqrt[4]{V_M L} &= \frac{9.42493}{4} = 2.35623 = \log_{10} L_g; L_g = 227.1 \text{ ft. at} \\ \text{Vol} &= 3,410,569 \text{ cu.ft.} \end{aligned}$$

$Y = (e)$  (cylindrical coef.) (fineness ratio)

$$Y = .978 \times .6961 \times 8.36 = 5.691$$

$$Z = \frac{L}{L_g} (\text{fineness ratio}) = \frac{L^2}{L_g D} = \frac{(758.3)^2}{227.1 \times 80.7} = \frac{575,020}{20,598} = 27.916$$

$$(Y + Z) = 5.691 + 27.916 = 33.607$$

$$\log_{10}(Y + Z) = 1.53643$$

Note:

[e,  $\frac{L}{D}$ ,  $\frac{4}{\pi D^2} L$ ,  $\frac{L}{L_g}$ , are dimensionless quantities and can be

calculated from any set of dimensions that pertain to the same volume.  $(Y + Z)$  - independent of volume.]

When  $L = 758.3$  ft. Vol. = 3,410,569 cu.ft.

$$\left( \frac{L \text{ at } 100000}{758.3} \right)^3 = \frac{100000}{3,410,569} = :02932$$

$$L \text{ at } 100000 = \sqrt[3]{(758.3)^3 \times .02932} = \sqrt[3]{12,785,000} = 233.83 \text{ ft.}$$

By  $\log_{10}$

$$\log \frac{758.3^3}{100000} = 3 \times 2.87984 = 8.63952$$

$$" .02932 \quad \begin{array}{r} 8.46716-10 \\ 3 \quad | \quad 7.10368 \\ \quad \quad \quad 2.36689 \end{array}$$

$$\log L \text{ at } 100000 \quad 2.36689 \quad L \text{ at } 100000 = 233.83 \text{ ft.}$$

$$\frac{\text{Desired Vol}}{100000} = \frac{5,000,000}{100000} = 50.$$

$$\begin{array}{rcl} \log (L \text{ at } 100,000)^3 & \text{as before} & 7.10668 \\ \text{"} & 50 & \underline{1.69897} \\ & & 3 | \underline{\underline{8.80565}} \\ \log L_{5,000,000} & & 3.93522 = 861.41 \text{ ft.} = \text{length} \\ & & \text{of desired hull.} \end{array}$$

Requirement 1:

$$L \text{ at } 100,000 \text{ ft.}^3 = 233.83 \text{ ft.}$$

$$L \text{ at } 800,000 \text{ ft.}^3 = 467.66 \text{ ft.}$$

$$L \text{ at } 6,400,000 \text{ ft.}^3 = 935.32 \text{ ft.}$$

$$L \text{ at } 5,000,000 \text{ ft.}^3 = 861.41 \text{ ft.}$$

$$VL \text{ at } 100,000 \& 100 \text{ ft./sec.} = 100 \times 233.83 = \\ 23383 \text{ ft.}^2/\text{sec.} \log_{10} VL = 4.36889$$

$$VL \text{ at } 800,000 \& 100 \text{ ft./sec.} = 100 \times 467.66 = \\ 46766 \text{ ft.}^2/\text{sec.} \log_{10} VL = 4.66992$$

$$VL \text{ at } 6,400,000 \& 100 \text{ ft./sec.} = 100 \times 935.32 = \\ 93532 \text{ ft.}^2/\text{sec.} \log_{10} VL = 4.97095$$

$$VL \text{ at } 5,000,000 \& 100 \text{ ft./sec.} = 100 \times 861.41 = \\ 86141 \text{ ft.}^2/\text{sec.} \log_{10} VL = 4.93522$$

Enter left-hand scale of Fig. 8 with  $\log_{10}(Y + Z) = 1.52643$   
and follow across to scale .3 cu.ft. Vol. (see dotted line,  
Fig. 8).

From .3 cu.ft. Vol., interpolate for slope and follow across  
to 100,000 cu.ft. scale (see dotted line).

From 100,000 cu.ft. scale, follow across, interpolating for  
slope, to 800,000 and 6,400,000 cu.ft. scales.

From 800,000 to 6,400,000 scale is a straight line (see dotted  
line solution of this problem in Fig. 8).

Pick off the following values of  $C_H$ , and take logs:

Volume	$C_H$	$\log_{10} C_H$
100,000	.02180	8.33846-10
800,000	.01654	8.21854-10
6,400,000	.01380	8.13988-10

Note: Figs. 7 and 8 are for a speed of 100 ft./sec.,  
 $\rho = .00237$  slugs/ft.<sup>3</sup>, and standard  $\rho/\mu$ . Enter Fig. 9  
with  $\log_{10} VL = 4.93523$  and from curve pick off  
 $\log_{10} C_H = 8.147-10$ . Whence  $C_H = .01403$  at 5,000,000  
cu.ft. and 100 ft./sec. Use this value in Requirement 2.

#### Requirement 2:

Bare hull drag at 100 ft./sec.  $\rho = .00237$  slugs/cu.ft.

$$\text{Drag} = C_H \frac{\rho}{2} (\text{Vol})^{2/3} V^2$$

$$L = 861.4, V = 100, VL = 86141 \text{ ft.}^2/\text{sec.}; \\ \log_{10} VL = 4.93523.$$

From Fig. 9 with  $\log_{10} VL = 4.93523$  pick off  $\log_{10} C_H = 8.147-10$ ;  
 $C_H = .01403$  as explained above.

$$\text{Drag} = .01403 \times \frac{.00237}{2} \times (5,000,000)^{2/3} \times 100^2 = 4860.5 \text{ lb.}$$

#### Requirement 3:

HP. absorbed in overcoming bare hull drag at 120 ft./sec.

$$L = 861.41 \text{ ft.}; V = 120 \text{ ft./sec.}; VL = 103369 \text{ ft.}^2/\text{sec.}, \\ \log_{10} VL = 5.01439$$

From Fig. 9 with  $\log_{10} VL = 5.01439$  pick off  
 $\log_{10} C_H = 8.132-10; C_H = .01355$

$$\text{Drag} = C_H \frac{\rho}{2} (\text{Vol})^{2/3} V^2 = .01355 \times \frac{.00237}{2} \times (5,000,000)^{2/3} \times 120^2 = \\ 6761.8 \text{ lb.}$$

$$\text{HP. absorbed} = \frac{\text{Drag} V}{550} = \frac{6761.8 \times 120}{550} = 1475.3 \text{ HP.}$$

Note: HP. to equip ship with =  $\frac{(\text{Hull Drag} + \text{External Drag}) V_{\max}}{550 \times \text{Propeller Efficiency}}$

## Symbols and Formulas

Length	$L$ ft.
Maximum diameter	$D$ ft.
Distance nose to max. dia.	$x$ ft.
Maximum radius	$r$ ft.
(Vol) - air volume	(Vol) cu.ft.
Eccentricity, nose ellipse	e no dimensions $e = \frac{\sqrt{x^2 - r^2}}{x}$ no dimensions
Geometric length	$L_g = \sqrt[4]{[(Vol) + \frac{\pi r^3}{3}] L}$ ft.
Cylindrical coef. (Cyl. Coef.)	$\frac{(Vol)}{\frac{\pi D^2 L}{4}} = \frac{\frac{4}{3} (Vol)}{\pi D^2 L}$ no dimensions
Fineness ratio	$L/D$ no dimensions
Pressure difference shape coef.	$Y = e (\text{Cyl. Coef.}) (L/D)$ no dimensions. $Y = e \left( \frac{\frac{4}{3} (Vol)}{\pi D^3} \right)$
Skin friction shape coef.	$Z = \frac{L}{L_g} \times \frac{L}{D} = \frac{L^2}{L_g D}$ no dimensions
Whole hull shape coef.	$(Y + Z)$
Virtual volume	$V_V = (Vol) + \frac{\pi r^3}{3}$ cu.ft.
Density	$\rho$ slugs/cu.ft.
Air speed	$V$ ft./sec.
VL	Air speed $\times$ length $\text{ft.}^2/\text{sec.}$
Drag	$R = C_H \frac{\rho}{2} (Vcl)^{2/3} V^2$ lb.

## Symbols and Formulas (Cont.)

Drag coef. of bare hull  $C_H$  no dimensions

Horsepower absorbed by drag  $R_f$ ; HP. =  $\frac{R_f V}{550}$

$$\left( \frac{\text{Length at Volume 1}}{\text{Length at Volume 2}} \right)^3 = \frac{\text{Volume 1}}{\text{Volume 2}}$$

PART II

	ITEM	BUILDER'S NUMBERS.	REMARKS.
CONTINUATION OF U.S. NAVY	1	U.S.N. "B"	NON KNEE, ONE CAR, ONE ENGINE, TOTAL 149 FUSELAGE TYPE ON CAR, BUMPER UNISURFACE AND BOW CAR, TWIN PROPELLERS, SURFACE, FLAT PLATE TYPE ON STERN ONLY.
	2	U.S.N. "C"	NON KNEE, TWO ENGINES, TOTAL DIVISIONED CAR, BUMPER INCLUDED IN CAR, CHAMBER ON BOWS, PUSHER PROPELLERS.
	3	U.S.N. "D"	NON KNEE, ONE ENGINE, TOTAL DIVISIONED CAR, BUMPER INCLUDED IN CAR, CHAMBER ON BOWS, PUSHER PROPELLERS.
	4	U.S.N. "E"	NON KNEE, ONE ENGINE, TOTAL DIVISIONED CAR, BUMPER INCLUDED IN CAR, CHAMBER ON BOWS, PUSHER PROPELLERS.
	5	U.S.N. "F"	NON KNEE, ONE ENGINE, TOTAL DIVISIONED CAR, BUMPER INCLUDED IN CAR, CHAMBER ON BOWS, PUSHER PROPELLERS.
	6	LZ-120 & 121 (EXCEPT L-120)	RIGID, TWO SMALL POWER CARS, ONE LARGE POWER CAR WITH TWO ENGINES ON ONE PROPELLER, CONTROL CAR ATTACHED TO HULL.
	7	LZ-124 U.S.S. LOS ANGELES (No WATER RECOVERY)	RIGID, ONE POWER CAR, CONTROL CAR ADJACENT TO HULL, SMALL AMOUNT OF EXTERNAL BRACING, WELL-LINED SURFACES ON STERN ONLY.
CONTINUATION OF U.S. NAVY	8	LZ-1	RIGID, TWO POWER CARS ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, EXTERNAL KEEL, BOW & STERN SURFACE, SMALL AMOUNT OF EXTERNAL BRACING, BOW TYPE SURFACES ON STERN, FLAT PLATE TYPE SURFACES ON BOW.
	9	LZ-4 & 5	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, EXTERNAL KEEL, BOW & STERN SURFACE, SMALL AMOUNT OF EXTERNAL BRACING, BOW TYPE SURFACES ON STERN, FLAT PLATE TYPE SURFACES ON BOW.
	10	LZ-7 & 8	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, TOTAL OF THREE ENGINES, LARGE EXTERNAL KEEL, NO BASSINIER SURFACE, QUADRUPLE SURFACES ON BOW, LARGE AMOUNT OF EXTERNAL BRACING, FOUR PROPELLERS ON OUTBOARD.
	11	LZ-10 & 12	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, TOTAL OF THREE ENGINES, LARGE EXTERNAL KEEL, NO BASSINIER SURFACE, QUADRUPLE SURFACES ON BOW, LARGE AMOUNT OF EXTERNAL BRACING, FOUR PROPELLERS ON OUTBOARD.
	12	LZ-15 & 16	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, TOTAL OF THREE ENGINES, LARGE EXTERNAL KEEL, NO BASSINIER SURFACE, QUADRUPLE SURFACES ON BOW, LARGE AMOUNT OF EXTERNAL BRACING, FOUR PROPELLERS ON OUTBOARD.
	13	LZ-22 & 23	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, TOTAL OF THREE ENGINES, LARGE EXTERNAL KEEL, NO BASSINIER SURFACE, QUADRUPLE SURFACES ON BOW, LARGE AMOUNT OF EXTERNAL BRACING, FOUR PROPELLERS ON OUTBOARD.
	14	LZ-24 To 37	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, TOTAL OF THREE ENGINES, LARGE EXTERNAL KEEL, NO BASSINIER SURFACE, QUADRUPLE SURFACES ON BOW, LARGE AMOUNT OF EXTERNAL BRACING, FOUR PROPELLERS ON OUTBOARD.
	15	LZ-36	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, LARGE SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	16	LZ-42 To 50	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, LARGE SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	17	LZ-59 To 61 & 64 To 71 (EXCEPT 60 & 70)	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	18	LZ-72 To 90 (EXCEPT 73, 77 & 81)	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	19	LZ-91 To 94	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	20	LZ-95 To 99	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	21	LZ-100 & 101	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	22	LZ-102	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	23	LZ-104	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	24	LZ-106 To 111	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
	25	LZ-112 To 114	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.
26	ZR-1 U.S.S. SHENANDOAH	RIGID, ONE POWER CAR ONE ENGINE EACH, ONE OF WHICH IS A CONTROL CAR, NO EXTERNAL KEEL, SMALL SURFACE, FLAT PLATE TYPE SURFACES ON STERN, SMALLER AMOUNT OF EXTERNAL BRACING & STRUTS, BOW TYPE SURFACES ON STERN.	

CALCULATIONS BY CLINTON H. HAVILL.  
LIEUT., U.S.NAVY.

PART II

ITEM	POWER CARS - SMALL				TWO ENGINE POWER CARS.				CONTROL CARS ADJ. TO HULL				% SEPARATE C
	MAX. CROSS SECT. AREA ONE CAR Sq.Ft.	CAR COEF.	AREA OF DRAG FOR POWER CAR. BOWKERON Sq.Ft.	NO OF CARS	TOTAL AREA OF DRAG FOR ALL CARS. Sq.Ft.	CROSS SECT. AREA (MAX)	CAR COEF.	AREA OF DRAG. POWER CAR Sq.Ft.	CROSS SECT. AREA (MAX)	CAR COEF.	AREA OF DRAG, (MAX) Sq.Ft.	CROSS SECT. AREA (MAX) Sq.Ft.	
1													23.11 .45
2													49.72 .40
3													49.72 .40
4													33.00 .41
5													33.00 .41
6	31	.32	9.92	2	19.84	42	.44	18.48	121.00	.11	13.31		
7	40 <sup>a</sup>	.30	12.00	5	60.00				176.84	.07	15.71		
8	36	.45	16.20	2	32.40								
9	38	.45	17.10	2	34.20								
10	40	.43	17.20	1	17.20								.46 .37
11	42	.43	18.06	1	18.06								.48 .37
12	43	.43	18.49	1	18.49								.49 .39
13	43	.43	18.49	1	18.49								.49 .39
14	45	.42	18.70	1	18.70								.51 .36
15	45	.41	18.45	1	18.45								.51 .36
16	42	.40	16.80	1	16.80	47	.45	21.15					.48 .35
17	37	.40	14.80	3	44.40								.43 .34
18	37	.40	14.80	2	29.60	47	.45	21.15					.43 .34
19	35	.40	14.00	3	42.00								.41 .39
20	35	.40	14.00	3	42.00								.41 .31
21	35	.40	14.00	3	42.00								.41 .31
22	35	.40	14.00	3	42.00								.41 .31
23	35	.40	14.00	3	42.00								.41 .31
24	35	.35	12.25	3	36.75								.41 .31
25	33.1	.33	10.92	5	54.60								.36 .30
26	34.3 <sup>a</sup>	.33	11.32	5	56.60								.36.16 .30

\* SOME HAVE ENGINES.

© EXTERNAL BUMPERS INCLUDED.

A MEASURED FROM PLANS.

\* INCLUDES EXTERNAL BRACINGS, OUTRIGGERS

NOTE:- IT IS TO BE NOTED THAT THIS DRAG CAN SO FAR ONLY BE COMPUTED FOR UMAX AS IT IS NOT KNOWN IF THE HULL DRAG VARIES AS U<sup>2</sup> OR U<sup>3</sup>. THE UMAX AND AREA OF DRAG FOR THE WHOLE SHIP AS GIVEN IN PART I, WERE ONLY AT THE POINT WHERE IT AGREES, SUCH AS HPMAX, UMAX, E & K AT UMAX. REYNOLDS LAW IS THAT "SIMILAR SHIPS HAVE THE SAME DRAG AND SAME UL". THE DATA THUS FAR WAS PLOTTED AGAINST A NUMBER OF FUNCTIONS AND AS SHIPS WERE DISSIMILAR A TERM EQUIVALENT TO UL WAS FINALLY OBTAINED. LOG  $\sqrt{(\text{AIR VOL} + \frac{L^2}{3}) (\text{LENGTH})}$ , U = VELOCITY IN FEET PER SECOND. TH FOR SIMILAR SHIPS THIS DEFINITION OF UL<sub>g</sub> APPLIES AND FOR DISSIMILAR SHIPS GIVES THE RESULTS OF PLOT I THE RESEARCH FOR THIS UL<sub>g</sub> TERM EXTENDED OVER A PERIOD OF ABOUT FIVE MONTHS.

TEST CASE	CONTROL SURFACES:												PRELIM. PLOT NO. 1.					
	AREA OF BOTH SIDES OF ALL CONTROL SURFACES	CORE	AREA OF DRAG	* AREA FOR FOREGOING DRAG AREA (POWER ON)	SUM OF TOTAL DRAG AREA FOR WHOLE SHIP	AREA OF DRAG OF HULL	U <sub>MAX</sub> (FROM PART I)	BARE HULL VIRTUAL VOL DRAG (FROM PART I)	LOG <sub>10</sub> VM	LENGTH (FROM PART I)	LOG <sub>10</sub> LENGTH	LOG <sub>10</sub> (VM/L)	GEOGRAPHIC LENGTH	LOG U <sub>MAX</sub>	LOG UL AT U <sub>MAX</sub>	BARE HULL DRAG AT U <sub>MAX</sub> LBS		
Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	Sq. Ft	FT.	FT.	FT.	FT.	LOG (GEOGRAPHIC LENGTH) / LOG (FT.)	LOG (VM/L)	LOG (VM)	LOG (UL)		
10.40	1370	.0072	9.87	27	48.27	87.40	38.13	69.00	215.1	90380	4.95607	163	2.21219	7.16824	1.79207	1.83885	3.63092	215.11
19.89	1969	.0072	14.17	34	67.80	127.37	59.57	88.00	546.9	189710	5.27807	196	2.29226	7.57035	1.89297	1.94448	3.83907	546.92
17.89	1969	.0072	14.17	34	67.80	131.46	63.66	83.11	521.0	199710	5.30040	198	2.29667	7.59707	1.89727	1.91965	3.81892	521.04
13.53	1125	.0072	8.10	17	36.63	78.00	41.37	82.20	331.2	99820	4.99922	162	2.20752	7.20874	1.80219	1.91487	3.71705	331.24
13.53	1125	.0072	8.10	17	38.09	79.01	40.96	77.30	290.0	99820	4.99922	162	2.20752	7.20874	1.80219	1.88818	3.67036	270.01
9.80	.0062	76.91	17	125.54	170.01	44.47	119.99	204.5	827920	5.91799	427	2.13043	8.54842	2.13711	2.07914	4.21625	204.50	
	8460	.0072	43.92	8	127.83	356.99	229.16	115.00	3891.2	22862061	6.45667	698.3	2.31842	9.27507	2.31877	2.06070	4.37947	3891.24
	1731	.0281	48.63	42	123.03	251.00	127.97	26.40	105.6	407310	5.60792	428	2.63124	8.24136	2.60334	1.42160	3.48194	105.66
	5357	.0281	150.55	42	226.75	383.01	156.26	41.00	311.2	982200	5.76507	446	2.14933	8.41440	2.10360	1.61278	3.71638	311.24
16.10	4651	.0273	126.98	40	200.28	374.00	173.72	51.98	555.8	746480	5.87312	486	2.18664	8.55976	2.13994	1.71984	3.89578	555.81
16.80	13530	.0242	327.41	35	397.27	563.00	169.73	62.40	764.8	643680	5.80867	460	2.16276	8.47153	2.11788	1.79518	3.91304	764.69
17.15	7197	.0240	171.77	35	242.41	412.00	169.59	67.50	915.8	797210	5.88036	466	2.16839	8.54875	2.13719	1.82930	3.96649	915.57
17.15	9773	.0238	233.08	32	300.44	482.00	181.56	66.69	955.2	802210	5.90428	512	2.17027	8.61355	2.15339	1.82406	3.77749	955.21
18.36	10720	.0238	255.08	30	322.44	409.00	86.56	70.89	512	873210	5.94111	519	2.1517	8.45628	2.16407	1.89058	4.01465	912.46
18.36	14750	.0065	97.23	19	153.04	333.98	145.79	77.09	1273.4	903040	5.79569	530	2.72428	8.67997	2.16979	1.88700	4.05699	1273.62
16.80	15920	.0068	108.29	25	187.99	393.00	205.01	81.61	1617.6	1250900	6.09722	536	2.72916	8.82638	2.20659	1.91174	4.11833	1617.67
14.62	13680	.0065	88.73	19	166.95	369.49	202.54	86.00	1775.1	1393900	6.14422	586	2.76790	8.91212	2.22803	1.93450	4.16253	1775.09
14.62	21110	.0071	149.91	19	234.28	474.00	239.72	92.42	2425.4	2211820	6.34473	645	2.80956	7.15429	2.23897	1.96767	4.25424	2425.07
15.99	15390	.0071	109.28	18	185.27	423.00	237.73	92.41	2405.4	2202820	6.34297	645	2.80956	7.15253	2.25813	1.96572	4.25385	2405.02
12.71	10510	.0063	64.27	15	133.98	372.00	236.02	96.19	2586.	2202820	6.34297	645	2.80956	7.15253	2.28813	1.98313	4.27126	2586.77
12.71	10260	.0063	64.62	15	134.33	371.00	236.67	97.40	2660.	2203820	6.34297	645	2.80956	7.15253	2.28813	1.98856	4.27669	2660.63
12.71	11280	.0063	71.09	17	142.76	419.00	276.24	94.29	2907.	2202820	6.43182	745	2.87216	7.30398	2.32599	1.97447	4.30446	2909.87
12.71	12060	.0063	75.99	18	148.70	424.00	275.30	94.19	2893.	2202820	6.43182	745	2.87216	7.30398	2.32599	1.97400	4.29999	2893.69
12.71	11180	.0063	70.49	17	134.95	372.00	235.05	104.81	3048.	2203820	6.34297	645	2.80956	7.15253	2.28813	2.02040	4.30893	3048.87
10.84	10600	.0062	67.77	16	147.21	404.00	256.79	113.12	3892.	2462820	6.39142	745	2.87216	7.26398	2.31589	2.05357	4.36943	3892.34
10.84	11304	.0062	70.08	17	152.52	402.51	249.99	91.00	2453.	2352481	6.37156	680.3	2.83264	7.20420	2.30105	1.95704	4.26009	2453.15

A<sub>x</sub>A<sub>TOTAL</sub>A<sub>H</sub> = A<sub>TOTAL</sub> - A<sub>x</sub>SEE NOTE  
AT TOP OF  
PAGE

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CALCULATIONS BY CLINTON H. HAVILL  
LIEUT., U.S. NAVY.

KNOTS ETC.

PART II

ITEM	U <sub>HULL</sub> FROM PART I FT./SEC	TOTAL AREA OF DRAG OF WHOLE SHIP POWER C/N	TOTAL DRAG OF WHOLE SHIP POWER C/N	% OF TOTAL DRAG AT HULL LEVEL (ESTIM. RATIO) *	3.42E HULL TOTAL DRAG AT HULL LEVEL LBS.	Log <sub>10</sub> UL UNITS AT UNLK.	PZELIN. PLOT - Z		VIRTUAL VOLUME V <sub>M</sub> FROM PART I CU. FT.	Log <sub>10</sub> V <sub>M</sub> LA FROM PART I FT.	ACTUAL LENGTH LA FROM PART I FT.	Log <sub>10</sub> LENGTH LA	Log <sub>10</sub> V <sub>M</sub> LA	Log <sub>10</sub> V <sub>M</sub> LA LOGIC LENGTH LA LOGIC L <sub>Y</sub>	U <sub>NAT</sub> =COM PART I FT., SEC	Log <sub>10</sub> UL <sub>Y</sub> @ UNLK. SOME AS UNLK IN PART I & 2 FT., SEC			3.42E HULL DRAG AT HULL LEVEL C/N Z	D <sub>H</sub> C/N
							V <sub>M</sub>	LA								Log <sub>10</sub> UL <sub>Y</sub> # UNLK. SOME AS UNLK IN PART I & 2 FT., SEC	Log <sub>10</sub> UL <sub>Y</sub> SOME AS UNLK IN PART I & 2 FT., SEC			
1	69.00	87.40	493.08	44	216.75	3.63092	90380	4.9560	163	2.21219	7.16826	1.77207	69.00	1.83885	3.63092	215	.01			
2	88.00	127.40	1167.09	47*	547.47	3.83707	189710	5.2780	196	2.29226	7.57035	1.87259	88.00	1.74448	3.83707	547	.01			
3	83.11	131.49	1076.06	48*	514.50	3.81892	199710	5.3004	198	2.29467	7.599707	1.89727	83.11	1.71905	3.81892	521	.01			
4	82.20	78.00	624.53	53	331.00	3.71709	99820	4.9992	162	2.20952	7.20874	1.80218	82.20	1.91487	3.71709	331	.01			
5	77.30	79.01	559.42	57	318.84	3.69036	99820	4.9992	162	2.20952	7.20874	1.80218	77.30	1.88818	3.69036	270	.02			
6	119.99	170.01	2898.50	60	1737.10	4.21625	827920	5.9177	427	2.63043	8.54842	2.13711	119.99	2.07914	4.21625	2110	.01			
7	115.00	356.97	5574.97	64*	3580.52	4.37947	2862061	6.4566	658.3	2.81842	9.27507	2.31877	115.00	2.06070	4.37947	370	.01			
8	26.40	251.00	267.26	51	105.70	3.48194	407310	5.6099	428	2.63144	8.24136	2.06034	26.40	1.42160	3.48194	106	.02			
9	41.00	383.01	762.92	41	312.79	3.71638	582200	5.7650	446	2.64933	8.41440	2.10360	41.00	1.61278	3.71638	311	.02			
10	51.98	374.00	1194.61	46	550.44	3.85578	746680	5.8731	486	2.68664	8.55976	2.13794	51.98	1.71584	3.85578	556	.02			
11	62.40	963.00	2577.85	43	1117.07	3.91304	643680	5.8084	460	2.66276	8.47153	2.11788	62.40	1.79518	3.91304	765	.02			
12	67.50	412.00	2224.31	41	911.76	3.96649	759210	5.8803	466	2.66839	8.54875	2.13719	67.50	1.82930	3.96649	916	.02			
13	66.69	482.00	2535.94	38	963.65	3.97745	802210	5.7042	512	2.70927	8.41355	2.15339	66.69	1.82406	3.97745	955	.02			
14	70.89	409.00	2421.52	46	1113.89	4.01465	873210	5.9411	517	2.71517	8.69428	2.16407	70.89	1.85058	4.01465	1090	.02			
15	77.09	333.98	2350.85	54	1269.46	4.05699	703040	5.9556	530	2.72428	8.67977	2.16999	77.09	1.88700	4.05699	1274	.01			
16	81.61	393.00	3101.08	52	1612.56	4.11833	1250900	6.0972	536	2.72916	8.82638	2.20459	81.61	1.91174	4.11833	1520	.01			
17	86.00	349.49	3238.28	59	1781.05	4.16253	1373900	6.1442	586	2.76790	8.91212	2.22803	86.00	1.93450	4.16253	1779	.01			
18	92.40	474.00	4775.13	51	2445.51	4.25424	2211820	6.3447	645	2.80956	9.15429	2.28897	92.40	1.96571	4.25424	2425	.01			
19	92.41	423.00	4279.49	56	2394.51	4.25385	2202820	6.3425	645	2.80976	9.15253	2.28813	92.41	1.96572	4.25385	2405	.01			
20	96.19	372.00	4077.12	63	2568.58	4.27126	2202820	6.3425	645	2.80956	9.15253	2.28813	96.19	1.98313	4.27126	2587	.01			
21	97.40	311.00	4170.78	64	2669.29	4.27669	2203820	6.3425	645	2.80956	9.15253	2.28813	97.40	1.98856	4.27669	2661	.01			
22	94.29	419.00	4413.75	66	2713.07	4.30046	2702820	6.4318	745	2.87216	9.30378	2.32599	94.29	1.97447	4.30046	2910	.01			
23	94.19	424.00	4456.66	65	2894.83	4.29999	2702820	6.4318	745	2.87216	9.30378	2.32599	94.19	1.97400	4.29999	2894	.01			
24	104.81	372.00	4851.25	63	3096.28	4.30853	2203820	6.3425	645	2.80956	9.15253	2.28813	104.81	2.02040	4.30853	3069	.01			
25	113.12	404.00	6123.83	63	3258.01	4.36743	2462820	6.3714	745	2.87216	9.26358	2.31789	113.12	2.05354	4.36743	3893	.01			
26	91.00	402.51	3949.43	62*	2448.64	4.26009	2372481	6.3715	680.2	2.83264	9.20420	2.30105	91.00	1.97904	4.26009	2480	.01			
					D <sub>H</sub>	V <sub>M</sub>		L <sub>A</sub>								D <sub>H</sub>	C			

COMPARISON OF BARE HULL  
DRAG AT 100 FT/SEC.

$\log_{10} UL_g$ @ 100 FT/SEC	BARE HULL DRAG AT 100 FT/SEC	DRAG COEF OF 3 SIZE HULL @ 100 FT/SEC	EXPLANATION
$= \log_{10} L_g + 2$	FROM PLOT #3	LBS	$C_H$
3.79207	420	.0185	COMPARISON OF SHIPS IF REDUCED OR EXPANDED TO THE SAME AIR VOLUME OF HULL. RELATION BETWEEN TWO SIMILAR
3.89259	640	.0170	SOLIDS OF LINEAR DIMENSIONS IN THE RATIO OF $\frac{L_1}{L_2}$ ARE AS FOLLOWS: - $\frac{VOL_1}{VOL_2} = \left(\frac{L_1}{L_2}\right)^3$ .
3.89927	660	.0167	FOR THE SAME OR GEOMETRICALLY SIMILAR
3.80218	432	.0175	AIRSHIP HULLS BUT OF DIFFERENT SIZES.
3.80218	432	.0175	$\frac{\text{AIR VOL. OF HULL}_1}{\text{AIR VOL. OF HULL}_2} = \left(\frac{\text{SIMILAR LINEAR DIMENSION}_1}{\text{SIMILAR LINEAR DIMENSION}_2}\right)^3 = \left(\frac{\text{GEOMETRIC LENGTH}_1}{\text{GEOMETRIC LENGTH}_2}\right)^3 \times \left(\frac{\text{L}_1}{\text{L}_2}\right)^3$ .
4.13711	1650	.0163	$\frac{\text{ACTUAL AIR VOL. OF HULL}}{\text{NEW AIR VOL. OF HULL}} = \left(\frac{\text{ACTUAL L}_g}{\text{NEW L}_g}\right)^3$
4.31877	3120	.0125	TO REDUCE ALL ITEMS TO 100,000 CU.FT. AIR VOL. OF HULL. $\frac{\text{ACTUAL AIR VOL. OF HULL}}{100000} = \left(\frac{\text{ACTUAL L}_g}{\text{NEW L}_g}\right)^3$ .
4.06034	1275	.0199	BY $\log_{10}$ .
4.10360	1460	.0179	$\log_{10}(NEW L_g) = \frac{1}{3} \log_{10} 100000 - \frac{1}{3} \log_{10}(\text{ACTUAL AIR VOL}) +$
4.13994	1640	.0171	$\log_{10}(\text{ACTUAL L}_g)$ .
4.11788	1530	.0164	$\log_{10}(\text{NEW L}_g) = \frac{5}{3} - \frac{1}{3} \log_{10}(\text{HULL VOL}) + (\log_{10} L_g \text{ AS TABULATED BEFORE})$
4.13719	1430	.0168	
4.15339	1700	.0169	
4.16407	1750	.0164	
4.16999	1775	.0163	
4.20659	1970	.0146	
4.22803	2110	.0145	
4.28857	2615	.0133	
4.28813	2615	.0133	
4.28813	2615	.0133	
4.28813	2615	.0133	
4.32599	3050	.0135	
4.32599	3050	.0135	
4.28813	2615	.0133	
4.31589	2905	.0137	
4.30105	2740	.0134	
	D_H	C_H	

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PART II

ITEM	AIR VOLUME OF HULL FROM PART I Cu.FT.	LOG <sub>10</sub> (AIR VOL) OF HULL	LOG <sub>10</sub> VOL	LOG <sub>10</sub> (Lg)AS TABULATED BEFORE FOR ACTUAL SIZE	LOG <sub>10</sub> Lg + LOG <sub>10</sub> 100000 Cu.FT. LOG Lg @ 100,000 = (LOG Lg + LOG LOG <sub>10</sub> Lg LOG <sub>10</sub> VOL)	LOG <sub>10</sub> Lg @ 100 FT AND 100,000 Cu VOLUME LOG <sub>10</sub> Lg LOG <sub>10</sub> VOL	
1	84000	4.92428	1.64143	1.79207	1.66667	3.45874	1.81731
2	180000	5.25921	1.75176	1.89259	-	3.55926	1.80750
3	190000	5.27875	1.75958	1.89927	-	3.56594	1.80636
4	95000	4.97772	1.65924	1.80218	-	3.46885	1.80961
5	95000	4.97772	1.65924	1.80218	-	3.46885	1.80961
6	797000	5.90146	1.76715	2.13711	-	3.80378	1.83663
7	2764461	6.44161	2.14720	2.31877	-	3.78544	1.83324
8	400000	5.60206	1.86735	2.06034	1.66667	3.72701	1.85966
9	572000	5.75740	1.91913	2.10360	-	3.77027	1.87114
10	734000	5.86574	1.95525	2.13974	-	3.80661	1.87136
11	631000	5.80003	1.93334	2.11788	-	3.78455	1.85121
12	741000	5.87157	1.95719	2.13719	-	3.80386	1.84667
13	787000	5.89797	1.96532	2.15339	-	3.82006	1.85474
14	858000	5.93349	1.97783	2.16407	-	3.83074	1.85291
15	884000	5.94645	1.98215	2.16997	-	3.83066	1.85451
16	1220000	6.08636	2.02879	2.20659	-	3.87326	1.84417
17	1363000	6.13450	2.04483	2.22803	-	3.89470	1.84987
18	2149000	6.33224	2.11075	2.28857	-	3.79524	1.84457
19	2140000	6.33041	2.11014	2.28813	-	3.75480	1.84466
20	2140000	6.33041	2.11014	2.28813	-	3.75480	1.84466
21	2141000	6.33062	2.11021	2.28813	-	3.75480	1.84459
22	2640000	6.42160	2.14053	2.32599	-	3.97244	1.85213
23	2640000	6.42160	2.14053	2.32599	-	3.97244	1.85213
24	2141000	6.33062	2.11021	2.28813	-	3.75480	1.84459
25	2400000	6.38021	2.12674	2.31589	-	3.78256	1.85582
26	2289861	6.35980	2.11793	2.30105	-	3.96772	1.84777

**PARTITION OF BARE HULLS AT VARYING AIR VOLUMES AND A VE**

000 Cu.Ft.		200,000 Cu.Ft.		400,000 Cu.Ft.		800,000	
D <sub>H</sub>	C <sub>H</sub>	Log <sub>10</sub> ULY	D <sub>H</sub>	C <sub>H</sub>	Log <sub>10</sub> ULY	D <sub>H</sub>	C <sub>H</sub>
FROM PLATE 3 BARE HULL DRAG @ 100 FT/SEC AND 200,000 CU.FT. AIR VOLUME (LBS)	D <sub>H</sub> = $\frac{2D_H}{C_H \cdot \log_10(VOL)}$ $C_H = .0000371D_H$	DRAG COEFF @ 100 FT/SEC AND 200,000 CU.FT. VOL. U = 100 VOL = 200,000 LOG ULY = 1.0034 LOG Z = .10034	FROM PLATE 3 BARE HULL DRAG @ 100 FT/SEC AND 200,000 CU.FT. VOL. U = 100 VOL = 200,000 LOG ULY = 1.0034 LOG Z = .10034	D <sub>H</sub> = $\frac{2D_H}{C_H \cdot \log_10(VOL)}$ $C_H = .0000371D_H$	DRAG COEFF @ 100 FT/SEC AND 400,000 CU.FT. VOL. U = 100 VOL = 400,000 LOG ULY = 1.0067 LOG Z = .10067	D <sub>H</sub> = $\frac{2D_H}{C_H \cdot \log_10(VOL)}$ $C_H = .0000371D_H$	DRAG COEFF @ 100 FT/SEC AND 800,000 CU.FT. VOL. U = 100 VOL = 800,000 LOG ULY = 1.0101 LOG Z = .10101
470	.01819	3.91765	730	.01801	4.01797	1090	.01695
475	.01811	3.90784	710	.01782	4.00818	1060	.01648
476	.01811	3.90670	705	.01739	4.00704	1056	.01642
480	.01820	3.90995	715	.01764	4.01029	1080	.01679
480	.01820	3.90995	715	.01764	4.01029	1080	.01679
540	.02115	3.93697	805	.01986	+03731	1188	.01847
540	.02115	3.93858	806	.01989	+03892	1190	.01850
595	.02331	3.96000	896	.02211	4.00034	1265	.01967
596	.02311	3.95142	880	.02171	4.05182	1230	.01913
597	.02315	3.95170	882	.02176	4.05204	1240	.01928
598	.02311	3.95154	880	.02171	4.05183	1238	.01925
599	.02233	3.94701	830	.02042	4.04135	1228	.01894
599	.02323	3.95508	885	.02182	4.05542	1245	.01936
599	.02319	3.95325	883	.02179	4.05359	1241	.01929
599	.02323	3.95485	885	.02184	4.05519	1245	.01936
568	.02225	3.94481	848	.02092	4.04515	1210	.01882
572	.02241	3.95021	852	.02102	4.05055	1212	.01885
560	.02194	3.94483	835	.02060	4.04517	1211	.01883
560	.02194	3.94500	835	.02060	4.04531	1213	.01886
560	.02194	3.94500	835	.02060	4.04534	1213	.01886
560	.02194	3.94493	835	.02060	4.04527	1213	.01886
582	.02279	3.95247	866	.02137	4.05281	1260	.01959
582	.02279	3.95247	864	.02137	4.05281	1260	.01959
560	.02194	3.94493	835	.02060	4.04527	1210	.01881
580	.02272	3.95616	865	.02134	4.05650	1260	.01959
570	.02233	3.94813	840	.02073	4.04847	1220	.01897
D <sub>H</sub>	C <sub>H</sub>						

## VELOCITY OF 100 FEET PER SECOND.

Cu. Ft.	1,600,000 Cu. Ft.	6,100,000 Cu. Ft.	LOG <sub>H</sub> D <sub>H</sub>	D <sub>H</sub>	C <sub>H</sub>	LOG <sub>H</sub> D <sub>H</sub>	D <sub>H</sub>	C <sub>H</sub>	LOG <sub>H</sub> D <sub>H</sub>	D <sub>H</sub>	C <sub>H</sub>
DRAG COEF OF BARE HULL DRAG Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> Vol = 6,100,000 C <sub>H</sub> = 0.00007725 D <sub>H</sub>	LOG <sub>H</sub> D <sub>H</sub> (@ 100 ft/sec) AND 1,600,000 Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)	LOG <sub>H</sub> D <sub>H</sub> (@ 100 ft/sec) AND 6,100,000 Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)	LOG <sub>H</sub> D <sub>H</sub> (@ 100 ft/sec) AND 6,100,000 Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)	D <sub>H</sub>	DRAG COEF OF BARE HULL DRAG Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)	D <sub>H</sub>	DRAG COEF OF BARE HULL DRAG Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)	D <sub>H</sub>	DRAG COEF OF BARE HULL DRAG Cu. Ft. Air Vol Cu. Ft. Air Vol Log Log S <sub>H</sub> = + Log D <sub>H</sub> (LBS)		
.01518	4.21868	2120	.01308	4.41937	5229	.01280	3.79207	420	.0135		
.01449	4.20807	2060	.01271	4.40756	4902	.01200	3.89259	640	.0176		
.01429	4.20773	2058	.01270	4.40842	4861	.01190	3.89727	660	.0175		
.01469	4.21098	2080	.01283	4.41167	5021	.01229	3.80218	432	.0176		
.01469	4.21098	2080	.01283	4.41167	5024	.01229	3.80218	432	.0176		
.01576	4.23800	2270	.01413	4.43847	5955	.01357	4.13711	1650	.0163		
.01605	4.23961	2285	.01409	4.44030	4943	.01210	4.31877	3120	.0125		
.01718	4.26103	2495	.01539	4.46172	5392	.01320	4.06034	1275	.0197		
.0167	4.25251	2422	.01594	4.45320	6209	.01520	4.10360	1460	.0179		
.0167	4.25273	2422	.01574	4.45342	6271	.01540	4.13794	1640	.0171		
.0167	4.25258	2422	.01594	4.45327	6250	.01530	4.11786	1530	.0162		
.0164	4.24804	2384	.01571	4.44273	6209	.01520	4.13719	1630	.0168		
.0168	4.25611	2428	.01498	4.45680	6154	.01460	4.15339	1700	.0169		
.0167	4.25428	2425	.01496	4.45427	6617	.01617	4.16407	1750	.0164		
.0168	4.25588	2425	.01498	4.45657	6195	.01589	4.16999	1775	.0163		
.0164	4.24584	2340	.01444	4.44653	6250	.01530	4.20659	1970	.0146		
.0166	4.23580	2435	.01487	4.45193	6168	.01509	4.22803	2110	.0145		
.0164	4.25124	2340	.01444	4.44655	5310	.01300	4.28857	2615	.0133		
.0165	4.24603	2380	.01468	4.44672	5310	.01300	4.28813	2615	.0133		
.0165	4.24603	2380	.01468	4.44672	5310	.01300	4.28813	2615	.0133		
.0165	4.24603	2378	.01467	4.44668	5310	.01300	4.28813	2615	.0133		
.0167	4.25350	2420	.01493	4.45414	5351	.01310	4.32599	3050	.0135		
.0167	4.25350	2420	.01493	4.45449	5351	.01310	4.32599	3050	.0135		
.0165	4.24574	2360	.01456	4.44665	5024	.01229	4.28813	2615	.0133		
.0168	4.25720	2425	.01494	4.45789	5310	.01300	4.31587	2905	.0137		
.0166	4.24714	2370	.01454	4.44785	5141	.01259	4.30105	2740	.0134		

 CALCULATIONS BY CLINTON H. HAVILL  
 LIEUT., U.S.NAVY.

A Shape Comparison Of Hull Dens. Curve & 100 Ft. Spec.										Preliminary Plot No. 5								
ITEM	Ecc. CYL.	WHEN THE SHIPS CONNECTED BY ARROWS ARE REQUIRED OF EXPANDED TO THE SAME VOLUME AS THE SHIP IDENTIFY THAT THE MEAN OF THEIR DENS. CAN BE TAKEN FOR DRY SP. WT.	MEAN EXCLUS. SECTION	MEAN VALUE OF DENS. CURVE ON HULL			LOG LENGTH	LOG LENGTH	LOG LENGTH	LOG LENGTH	LOG LENGTH	PREVIOUS COMPARISON SHIPS COMPARED ACCORDING TO "Z"			MEAN VALUE OF DENS. CURVE ON HULL	MEAN VAL. OF DENS. ON SHIPS CONNECTED		
				@ Cu. Ft. Vol.	@ Cu. Ft. Vol.	@ Cu. Ft. Vol.						LOG LENGTH						
1	4.21	→	4.21	.01823	.01422	.01322	1.77207	2.21219	4.2012	2.631	5.04	[3.31]			.01919	.01518	.01280	13.31
2	3.84	←	3.63	.01707	.01293	.01210	1.89279	2.29224	3.9967	2.910	4.62	[11.71]			.01851	.01439	.01175	11.71
3	3.49						1.87227	2.27067	3.9740	2.509	4.72	[11.84]						
4	3.10	→	3.10	.01740	.01329	.01240	1.80218	2.20952	4.0734	2.593	4.84	[12.37]			.01880	.01467	.01229	12.37
5	3.10	←					1.80218	2.20952	4.0734	2.593	4.84	[12.37]						
6	4.04	→	4.32	.01792	.01378	.01297	2.13711	2.63043	4.7332	3.113	6.70	[20.86]						
7	4.61	←					2.31877	2.81842	4.7769	3.160	7.29	[22.91]			.02115	.01600	.01284	21.87
8	7.20	→	7.27	.02232	.01638	.01424	2.06034	2.631	5.710	3.70	10.21	[8.81]						
9	7.21	←	9.39	.02341	.01641	.01562	2.10360	2.74933	5.4773	3.513	10.70	[30.87]						
10	7.76	←					2.13994	2.68664	5.4470	3.522	10.40	[37.33]						
11	8.14						2.11784	2.66274	5.4440	3.507	10.00	[35.07]						
12	8.02	→	8.24	.02314	.01623	.01571	2.13719	2.66837	5.3120	3.378	9.93	[32.48]						
13	8.45						2.15337	2.70927	5.5988	3.576	10.48	[37.67]						
14	8.21						2.14407	2.71517	5.5108	3.557	10.41	[37.74]						
15	7.55						2.16999	2.72428	5.5427	3.583	10.08	[36.12]						
16	6.34						2.20659	2.72914	5.2257	3.331	8.48	[28.91]						
17	7.05						2.22283	2.71770	5.3787	3.466	9.50	[32.73]						
18	5.55						2.28897	2.80972	5.2079	3.319	8.24	[27.35]						
19	5.52	→	5.53	.01964	.01631	.01314	2.28813	2.80974	5.2143	3.322	8.24	[27.37]						
20	5.52	←					2.28813	2.80974	5.2143	3.322	8.24	[27.37]						
21	5.53						2.28813	2.80976	5.2143	3.322	8.24	[27.37]						
22	5.89	→	5.87	.02019	.01654	.01316	2.32599	2.87216	5.4617	3.917	10.12							
23	5.87	←					2.32599	2.87216	5.4617	3.917	10.12							
24	5.53						2.28813	2.80976	5.2143	3.322	8.24	[27.37]						
25	6.38	→	6.37	.02012	.01662	.01324	2.31984	2.87216	5.6622	3.600	10.27							
26	5.84	→					2.36107	2.83264	5.34	3.71	8.44	[27.38]						
	"Y"											Z						

\* Ecc. x Cyl. = (Eccentricity Of Nose Ellipse) x (Cylindrical Coefficient) (Fineness Ratio).

CALCULATIONS BY CLINTON H. HAVILE  
LIEUT. U.S. NAVY.

PRISMATIC CRAFT. V	VOLUMETRIC DRAG COEF. (Model Tests) C <sub>H</sub>	MODEL DRAG @ STANDARD DENSITY-6025 ft <sup>3</sup> /sec						MODEL RADIUS r <sup>3</sup> IN. DIA. z (ft.)	MODEL r <sup>3</sup> (ft. <sup>3</sup> )	MODEL ADDITIONAL VOLUME x r <sup>3</sup> (cu. ft.)	MODEL VOLUME V cu. ft.
		C <sub>D</sub> 20 MI/H.R. 27.334 ft. <sup>2</sup> /sec	C <sub>D</sub> 40 MI/H.R. 58.667 ft. <sup>2</sup> /sec	C <sub>D</sub> 60 MI/H.R. 88 ft. <sup>2</sup> /sec	C <sub>D</sub> 20 MI/H.R. 27.334 ft. <sup>2</sup> /sec	C <sub>D</sub> 40 MI/H.R. 58.667 ft. <sup>2</sup> /sec	C <sub>D</sub> 60 MI/H.R. 88 ft. <sup>2</sup> /sec				
.17	.8	.9	10	11	12	13	14	.15	.16	.17	.8304
.6175	.0336	.0308	.0296	.0303	.0111	.2404	.34835	.042273	.044268	.6259	.6259
.6562	.0318	.0288	.0272	.0237	.0859	.1828	.32085	.033029	.034588	.6690	.6690
.6621	.0336	.0292	.0284	.0262	.0911	.1996	.32085	.033029	.034588	.5890	.5890
.5891	.0332	.0294	.0276	.0238	.0842	.1779	.32085	.033029	.034588	.7240	.7240
.5679	.0370	.0348	.0330	.0305	.1145	.2440	.32085	.033029	.034588	.5871	.5871
.5677	.0362	.0340	.0328	.0260	.0975	.2117	.32085	.033029	.034588	.6331	.6331
.6095	.0358	.0338	.0322	.0269	.1017	.2180	.32085	.033029	.034588	.3196	.3196
.6003	.0410	.0510	.0554	.0196	.0973	.2380	.29165	.024809	.025780	.6777	.6777
.6747	.0308	.0280	.0264	.0243	.0881	.1869	.32085	.033029	.034588	.7277	.7277
.7184	.0328	.0292	.0272	.0296	.1055	.2210	.32085	.033029	.034588	.8330	.8330
.7611	.0350	.0300	.0272	.0366	.1253	.2572	.32085	.033029	.034588	.1.0404	.1.0404
.7925	.0346	.0312	.0296	.0406	.1465	.3147	.32085	.033029	.034588	.1.2471	.1.2471
.8167	.0350	.0314	.0292	.0458	.1641	.3446	.32085	.033029	.034588	.1.4548	.1.4548
.8358	.0328	.0308	.0296	.0470	.1765	.3814	.32085	.033029	.034588	.1.6625	.1.6625
.8556	.03355	.03122	.03004	.0393	.1454	.3140	.32810	.035321	.036988	.1.2335	.1.2335
.7009	.03442	.03077	.02917	.0423	.1514	.3229	.32810	.035321	.036988	.1.3250	.1.3250

DRAG @ LOG <sub>10</sub> DL <sub>g</sub> @ 58.667 ft. sec. (L <sub>g</sub> )	DRAG @ LOG <sub>10</sub> DL <sub>g</sub> @ 88 ft. sec. (L <sub>g</sub> )	TO REDUCE OR EXPAND ALL MODELS TO THE SAME VOLUME.	$\frac{1}{3} \log_{10} .3$	LOG <sub>10</sub> L <sub>g</sub>	$\frac{1}{3} \log_{10} (\text{Vol. Mod})$	LOG <sub>10</sub> L <sub>g</sub> @ 3 cu. ft. Vol.
.33	.34	.35		.36	.37	.38
.1111	.206679	.2404	9.82571-10	.12231	.9.97309-10	.9.79493-10
.0859	.201636	.1828	*	.07238	.9.93217-10	.9.96597-10
.0911	.203002	.1996	*	.08554	.9.94181-10	.9.96944-10
.0842	.201576	.1779	*	.07128	.9.92337-10	.9.97362-10
.1145	.206341	.2440	*	.11893	.9.95325-10	.9.99139-10
.0975	.201978	.2117	*	.07530	.9.92337-10	.9.97764-10
.1017	.202709	.2180	*	.08260	.9.93382-10	.9.97449-10
.0973	.1.90394	.2380	*	.9.75946-10	.9.93487-10	.9.95030-10
.0881	.203084	.1869	*	.08632	.9.94368-10	.9.96835-10
.0936	.204393	.2013	X Mod.	.09945	.9.75438-10	.9.97078-10
.1055	.206783	.2210	X Mod.	.12335	.9.97355-10	.9.97551-10
.1253	.210897	.2572	X Mod.	.16449	.00573	.9.98447-10
.1465	.214328	.3147	X Mod.	.19888	.03197	.9.99262-10
.1641	.217312	.3446	X Mod.	.22864	.05424	.00011
.1765	.219927	.3814	X Mod.	.25479	.07389	.00691
.1454	.1.97693	.3140	X Mod.	.20853	.03038	.00386
.1514	.1.98988	.3229	X Mod.	.22148	.04074	.00645

MODEL V <sub>M</sub> = V + $\frac{UL^2}{3}$ Cu. Ft.	MODEL LENGTH (Ft.)	MODEL LOG <sub>10</sub> VIRT. VOL (LOG <sub>10</sub> V <sub>M</sub> )	MODEL LOG <sub>10</sub> LENGTH (LOG <sub>10</sub> L)	MODEL LOG <sub>10</sub> (V <sub>M</sub> L) (LOG <sub>10</sub> L)	MODEL LOG <sub>10</sub> $\sqrt[4]{V_M L}$ = LOG <sub>10</sub> Lg.	MODEL LOG <sub>10</sub> $\sqrt[4]{V_M L}$ = LOG <sub>10</sub> Lg.
18	19	20	21	22	23	24
.87467	3.527	9.74184-10	.54741	.48925	.12231	1.46737
.66049	2.949	9.81986-10	.46967	.28953	.07238	"
.70359	3.125	9.84732-10	.49485	.34217	.08554	"
.62359	3.092	9.77490-10	.49024	.28514	.07128	"
.75859	3.942	9.88000-10	.59572	.47572	.11893	"
.62369	3.208	9.79497-10	.50623	.30120	.07530	"
.66769	3.205	9.82457-10	.50583	.33040	.08260	"
.34558	1.992	9.53855-10	.29929	9.83784-10	9.95946-10	"
.71224	3.109	9.85265-10	.49262	.34527	.08632	"
.76429	3.270	9.88325-10	.5145	.39780	.09745	"
.86759	3.590	9.93832-10	.55509	.49341	.12335	"
1.07499	4.232	.03141	.62655	.65796	.16449	"
1.28169	4.872	.10779	.68771	.79550	.19888	"
1.48939	5.515	.17301	.74155	.91456	.22864	"
1.69709	6.158	.22972	.78944	.1.01916	.25479	"
1.27049	5.372	.10398	.73014	.83412	.20853	"
1.36199	5.646	.13418	.75174	.88592	.22148	"

\* FROM POINTS OF EACH PLOTTED ON FIGURE 6. NOT FROM SMOOTH MEAN CURVE.

#### CALCULATION OF ECCENTRICITY OF NOSE ELLIPSE. (x)

MODEL LOG <sub>10</sub> ULY @ 3 Cu. Ft. Vol LOG <sub>10</sub> F <sub>1</sub> Vol (LOG <sub>10</sub> L + 2)	HULL DRAFT 100 FT./SEC 3 Cu. Ft. Vol D <sub>H</sub> (L <sub>H</sub> ) C <sub>H</sub> = 1883 D <sub>H</sub>	X <sup>2</sup> 100 FT./SEC 3 Cu. Ft. Vol D <sub>H</sub> (L <sub>H</sub> ) C <sub>H</sub> = 1883 D <sub>H</sub>	DIST. FROM NOSE TO MAX. ORDINATE X (FT.)	X <sup>2</sup> 100 FT./SEC 3 Cu. Ft. Vol D <sub>H</sub> (L <sub>H</sub> ) C <sub>H</sub> = 1883 D <sub>H</sub>	$\frac{M_{H1} 2d}{Z}$ RAY. PHOT. T (FT.)	T <sup>2</sup> (FT.)	X <sup>2</sup> -T <sup>2</sup> RAY. PHOT. T (FT.)	$\sqrt[3]{X^2-T^2}$ RAY. PHOT. T (FT.)	$\frac{X}{\sqrt[3]{X^2-T^2}}$ RAY. PHOT. T (FT.)
40	41	42	43	44	45	46	47	48	49
1.77493	.1598	.0301	1.333	1.7729	.3483	.12131	1.67159	1.2853	.764
1.76572	.1492	.0281	.889	.7832	.3208	.10291	.68029	.8248	.732
1.76944	.1540	.0290	1.133	1.2837	.3208	.10291	1.18079	1.0867	.759
1.77362	.1508	.0285	1.283	1.6461	.3208	.10291	1.94319	1.2472	.768
1.79139	.1779	.0335	1.527	2.3317	.3208	.10291	2.22879	1.4909	.776
1.77764	.1583	.0298	1.161	1.3479	.3208	.10291	1.24499	1.1155	.760
1.77449	.1540	.0290	1.147	1.3154	.3208	.10291	1.21269	1.1101	.767
1.75030	.2719	.0512	.847	.7174	.2916	.08503	.63237	.7953	.738
1.76835	.1439	.0271	.885	.7832	.3208	.10291	.68029	.8248	.732
1.77078	.1450	.0273	.885	.7832	.3208	.10291	.68029	.8248	.732
1.77551	.1556	.0274	.885	.7832	.3208	.10291	.68029	.8248	.732
1.78447	.1597	.0281	.885	.7832	.3208	.10291	.68029	.8248	.732
1.77262	.1607	.0302	.885	.7832	.3208	.10291	.68029	.8248	.732
2.00011	.1640	.0308	.885	.7832	.3208	.10291	.68029	.8248	.732
2.00671	.1667	.0314	.885	.7832	.3208	.10291	.68029	.8248	.732
2.00386	.1629	.0306	2.015	4.0602	.3281	.10765	3.95255	.9831	.786
2.00445	.1644	.0307	2.015	4.0602	.3281	.10765	3.95255	.9831	.786

$C_{HY}$ 800,000 Cu.Ft. From Fig. 4	$C_{HY}$ 6,400,000 Cu.Ft. From Fig. 4	$YC_{HY}$ 800,000 Cu.Ft.	$YC_{HY}$ 6,400,000 Cu.Ft.	$Z$ (1.5 SECUND)	$C_{HZ}$ 800,000 Cu.Ft. From Fig. 5	$C_{HZ}$ 6,400,000 Cu.Ft. From Fig. 5	$C_{HZ}$ 100,000 Cu.Ft. From Fig. 5	$ZC_{HZ}$ 100,000 Cu.Ft.	
.59	.60	.61	.62	.63	.64	.65	.66	.67	.68
.0134	.0125	.052711	.040362	.037652	13.465	.0191	.0149	.0125	.25701
.0135	.0125	.049728	.038144	.039319	11.531	.0184	.0145	.0118	.21217
.0133	.0124	.053804	.041124	.038343	12.496	.0188	.0147	.0122	.23492
.0136	.0127	.048650	.037381	.034907	12.647	.0187	.0148	.0123	.23907
.0130	.0121	.058195	.044242	.041179	18.408	.0206	.0156	.0129	.37920
.0137	.0128	.048679	.037257	.034809	13.498	.0192	.0149	.0124	.25839
.0135	.0128	.050880	.039704	.037645	13.224	.0191	.0148	.0123	.25258
.0171	.0154	.040322	.032834	.029569	7.457	.0331	.0280	.0227	.24683
.0133	.0124	.053082	.040574	.037827	12.362	.0187	.0147	.0121	.23117
.0131	.0122	.056485	.043020	.040065	13.262	.0192	.0148	.0124	.25468
.0130	.0121	.064146	.048482	.045126	15.050	.0197	.0152	.0127	.29648
.0150	.0131	.088484	.070226	.061330	19.127	.0208	.0157	.0129	.39784
.0163	.0129	.109878	.091379	.072318	23.392	.0214	.0162	.01295	.50059
.0166	.0134	.136685	.108564	.087636	27.786	.0220	.0165	.0130	.61569
.0162	.0145	.167509	.121145	.108432	32.880	.0227	.0168	.0132	.74638
.0164	.0129	.108461	.090753	.071385	27.210	.0218	.0164	.0130	.59318
.0166	.0131	.118922	.098706	.077874	29.174	.0221	.0166	.01305	.64479

REMARKS	DATA FROM ORIGINAL LIST OF SHIPS FOR POINTS BETWEEN 100,000 AND 6,400,000 CU.FT. VOLUME WHERE WIND TUNNEL DATA ARE NOT AVAILABLE.	"Y"	Log. L Or Act. Ship
CONTINUOUS CURVATURE	BODENSEE LOS ANGELES	4.04 4.61	2.13711 2.31877
	LZ-1.	7.20	2.06034
	LZ-4 & 5.	9.21	2.10340
	LZ-7 & 8.	9.76	2.13974
	LZ-10 & 12.	8.14	2.11786
	LZ-15 & 16.	8.12	2.13717
	LZ-22 & 23.	8.45	2.15339
	LZ-24 To 35.	9.21	2.16407
	LZ-36.	7.55	2.16999
	LZ-42 To 50.	6.34	2.20658
PARALLEL SECTION	LZ-59 To 61, 64 To 71 EXCEPT 60 & 70.	7.05	2.22803
	LZ-72 To 90 EXCEPT 73-77 & 81.	5.55	2.28851
	LZ-91 To 94.	5.52	2.28813
	LZ-95 To 99.	5.52	2.28813
	LZ-100 & 101.	5.53	2.28813
	LZ-102.	5.89	2.32596
	LZ-104.	5.89	2.32596
	LZ-106 To 111.	5.53	2.28813
	LZ-112 To 114.	6.38	2.31589

$ZC_{HZ}$ @ 800,000 Cu.Ft.	$ZC_{HZ}$ @ 1,400,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 100,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 800,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 1,400,000 Cu.Ft. (As Before)	"Y" + "Z"	$YC_{HY} + ZC_{HZ}$ @ 100,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 800,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 1,400,000 Cu.Ft.
69	70	71	72	73	74	75	76	77
.20049	.16820	.30972	.24089	.20585	16.468	.01881	.01459	.01247
.16720	.13607	.26189	.20534	.17139	14.356	.01824	.01430	.01193
.18369	.15245	.28812	.22482	.19079	15.588	.01878	.01442	.01223
.18720	.15558	.28772	.22458	.19049	15.396	.01868	.01448	.01238
.28716	.23746	.43739	.33140	.27864	21.811	.02019	.01519	.01278
.20052	.16688	.30707	.23178	.20169	16.177	.01880	.01458	.01245
.19572	.16265	.30346	.23542	.20029	16.165	.01874	.01458	.01236
.20879	.16927	.28715	.24162	.19884	9.377	.03620	.02600	.02120
.18172	.14958	.28425	.22229	.18741	15.413	.01842	.01442	.01215
.19632	.16449	.31116	.23934	.20456	16.548	.01880	.01446	.01236
.22876	.19135	.36063	.27724	.23648	18.779	.01939	.01478	.01259
.30029	.24674	.48632	.37092	.30807	23.809	.02042	.01542	.01288
.31895	.30293	.61047	.47033	.37525	28.998	.02120	.01622	.01294
.46177	.36382	.75238	.57033	.49146	34.346	.02190	.01661	.01340
.55238	.43402	.91389	.67353	.54245	40.358	.02263	.01668	.01344
.44624	.35373	.70164	.53699	.42512	32.744	.02164	.01647	.01303
.48432	.38074	.76371	.58303	.45863	35.122	.02201	.01666	.01317

$\log_{10} L$ (Or Act. Size)	$\log_{10} \left(\frac{L}{L_g}\right)$	$\frac{L}{L_g}$	$\frac{L}{D}$	"Z"	"Y" + "Z"	$YC_{HY} + ZC_{HZ}$ @ 100,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 800,000 Cu.Ft.	$YC_{HY} + ZC_{HZ}$ @ 1,400,000 Cu.Ft.
Z.63043	.49332	3.1140	6.70	20.864	24.904	.02070	.01522	.01280
Z.81842	.49765	3.1598	7.25	29.086	33.696	.02480	.01610	.01300
Z.63144	.57110	3.7247	10.21	38.029	45.229	.02320	.01673	.01362
Z.64933	.54570	3.5132	10.50	36.888	46.398	.02420	.01699	.01392
Z.68664	.54670	3.5212	10.60	37.325	47.085	.02490	.01720	.01400
Z.66276	.54490	3.5065	10.00	39.065	43.205	.02310	.01670	.01356
Z.66837	.53120	3.3979	7.55	32.450	40.570	.02290	.01700	.01380
Z.70927	.55588	3.5947	10.48	37.693	46.143	.02410	.01690	.01380
Z.71517	.55110	3.5571	10.61	37.741	46.951	.02430	.01720	.01405
Z.72428	.55429	3.5835	10.08	36.122	43.672	.02320	.01680	.01360
Z.72916	.52257	3.3310	8.68	28.913	39.273			
Z.76790	.53987	3.4465	9.50	32.732	39.982	.02262	.01661	.01342
Z.80956	.52079	3.3189	8.24	27.348	32.898	.02164	.01648	.01304
Z.80956	.52144	3.3225	8.24	27.377	32.907	.02165	.01648	.01304
Z.80956	.52144	3.3225	8.24	27.377	32.907	.02165	.01648	.01304
Z.80956	.52144	3.3225	8.24	27.377	32.907	.02165	.01648	.01304
Z.87216	.54617	3.5170	9.52	33.482	37.372	.02268	.01668	.01349
Z.80956	.52144	3.3225	8.24	27.377	32.907	.02165	.01648	.01304
Z.87216	.54617	3.5170	9.52	33.482	37.372	.02268	.01668	.01349
Z.80956	.52144	3.3225	8.24	27.377	32.907	.02165	.01648	.01304
Z.87216	.55627	3.5998	9.52	34.270	40.650	.02270	.01670	.01350

## NOTES.

THE SCALES ON FIGURES 7 & 8 WERE PLOTTED WITH  $\log_{10}(Y+Z)$  A UNIFORM SCALE OF LOGARITHMS. THE MODEL SCALE WAS CONSTRUCTED NEARLY UNIFORM AND THE SCALE @100,000 WAS CALIBRATED ON THIS DATA. THE SCALE @6,400,000 WAS CONSTRUCTED NEARLY UNIFORM AND THE SLOPE LINES DRAWN IN FROM SCALE @100,000. THE SCALE @300,000 WAS ALLOWED TO CALIBRATE ITSELF ON THE DATA GIVEN HERE. CURVES OF THE SCALES WERE DRAWN AND THE GRADUATIONS MARKED WERE TRANSFERRED BACK TO THE SCALE.

IT IS THUS SEEN THAT THE SCALES ARE EMPIRICALLY CALIBRATED ON THE DATA HERE, MAKING THE SLOPE LINES STRAIGHT LINES AND GRADUATING THE SCALES ACCORDINGLY.

CALCULATIONS BY CLINTON H. HAVILL  
LIEUT, U.S.NAVY.

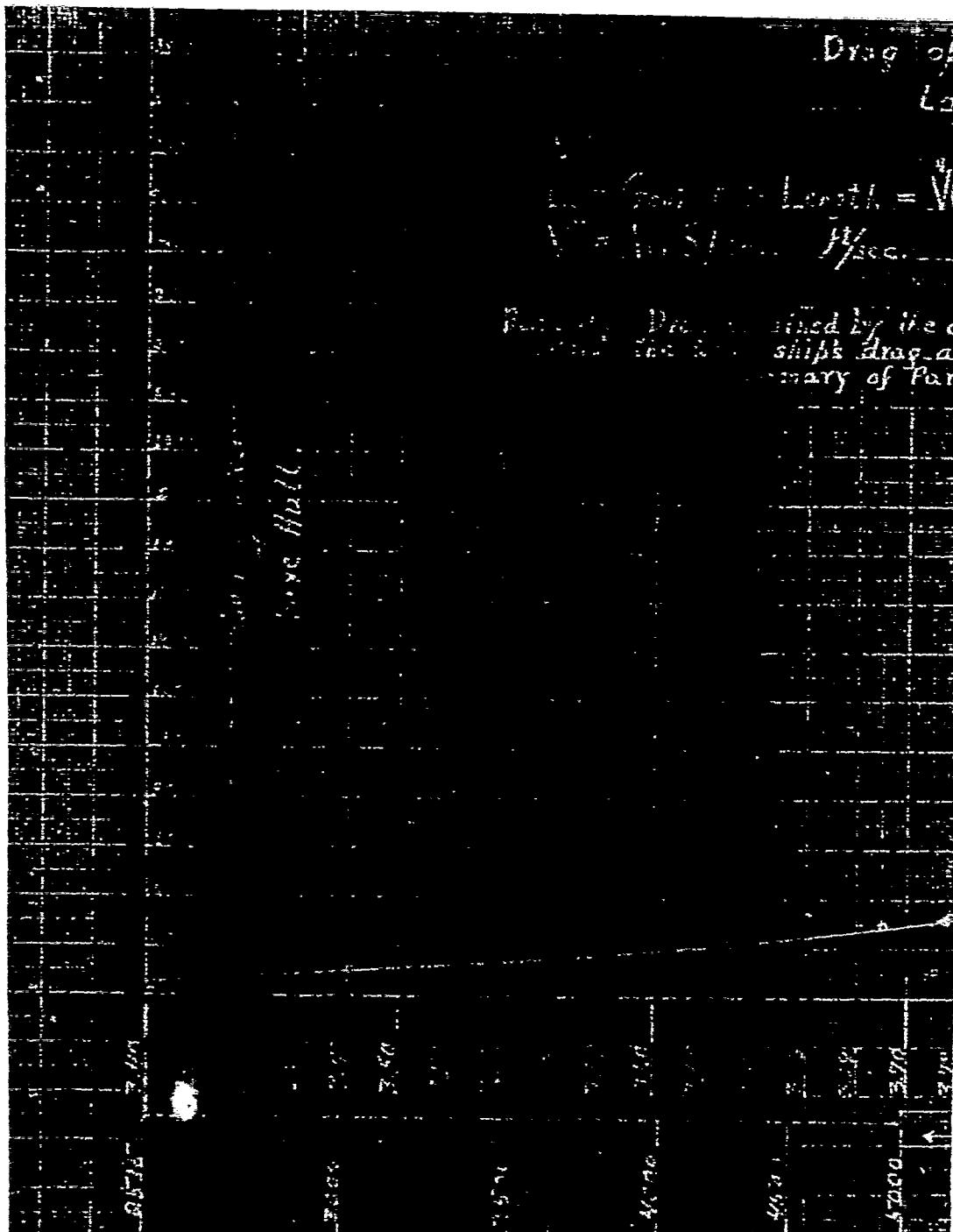
**FINAL SUMMARY OF PART II**  
 ARRANGEMENT OF PREVIOUS DATA IN ASCENDING VALUES OF "Y+Z"

CONTINUOUS CURVATURE SECTION	SHIPS	"Y"+"Z"	DRAG COEFFICIENT - $C_D$			
			@ .3 Cu.Ft.	@ 100,000 Cu.Ft.	@ 500,000 Cu.Ft.	@ 1,400,000 Cu.Ft.
"AA"		9.377	.0512	.03620	.02600	.02120
"C"		14.356	.0280	.01824	.01430	.01173
"EP"		15.396	.0285	.01868	.01442	.01228
"F"		15.588	.0290	.01878	.01449	.01233
"P-3"		16.165	.0295	.01880	.01458	.01236
"P-2"		16.177	.0298	.01881	.01458	.01245
"B"		16.468	.0301	.01882	.01459	.01247
"P-1"		21.811	.0335	.02019	.01519	.01278
BODENSEE		24.704		.02070	.01522	.01280
LOS ANGELES		33.676		.02480	.01610	.01300
"C + 1/4 DIA."		15.413	.0271	.01842	.01442	.01217
"C + 1/2 DIA."		16.548	.0274	.01830	.01446	.01236
"C + 1 DIA."		18.779	.02819	.01937	.01478	.01257
"C + 2 DIA."		23.807	.02938	.02042	.01542	.01288
"C + 3 DIA."		23.998	.03026	.02120	.01622	.01274
SHRWT SHENANDOAH		32.744	.03068	.02164	.01647	.01303
LZ-72 To 90 EXCEPT 73, 77 & 81.		32.898		.02164	.01648	.01304
LZ-91 To 94, 95 To 99, 100, 101 & 106 To 111		32.907		.02168	.01649	.01305
"C + 4 DIA."		34.346	.03088	.02190	.01661	.01340
SHENANDOAH.		35.122	.03090	.02201	.01666	.01347
LZ-42 To 50.		35.273		.02238	.01666	.01348
LZ-102 & 104.		39.372		.02258	.01667	.01349
LZ-59 To 61, 64 To 71 EXCEPT 60 & 70.		39.782		.02262	.01668	.01347
"C + 5 DIA."		40.398	.0314	.02263	.01668	.01344
LZ-112 To 114.		40.650		.02270	.01670	.01350
LZ-10 & 12.		43.205		.02310	.01680	.01356
LZ-1.		45.227		.02320	.01683	.01362
LZ-4 & 5.		46.378		.02420	.01699	.01372
LZ-7 & 8.		47.085		.02490	.01720	.01400

Drag of  
Log

$$D = \frac{C_D}{2} \rho A L^2 = \frac{C_D}{2} \rho A L^2$$
$$\text{where } C_D = 1.2 \text{ for } S_{\text{ref}} = 0.5 \text{ sec.}$$

Fig. 10. Drag produced by the drag of the ship's hull. Summary of Part



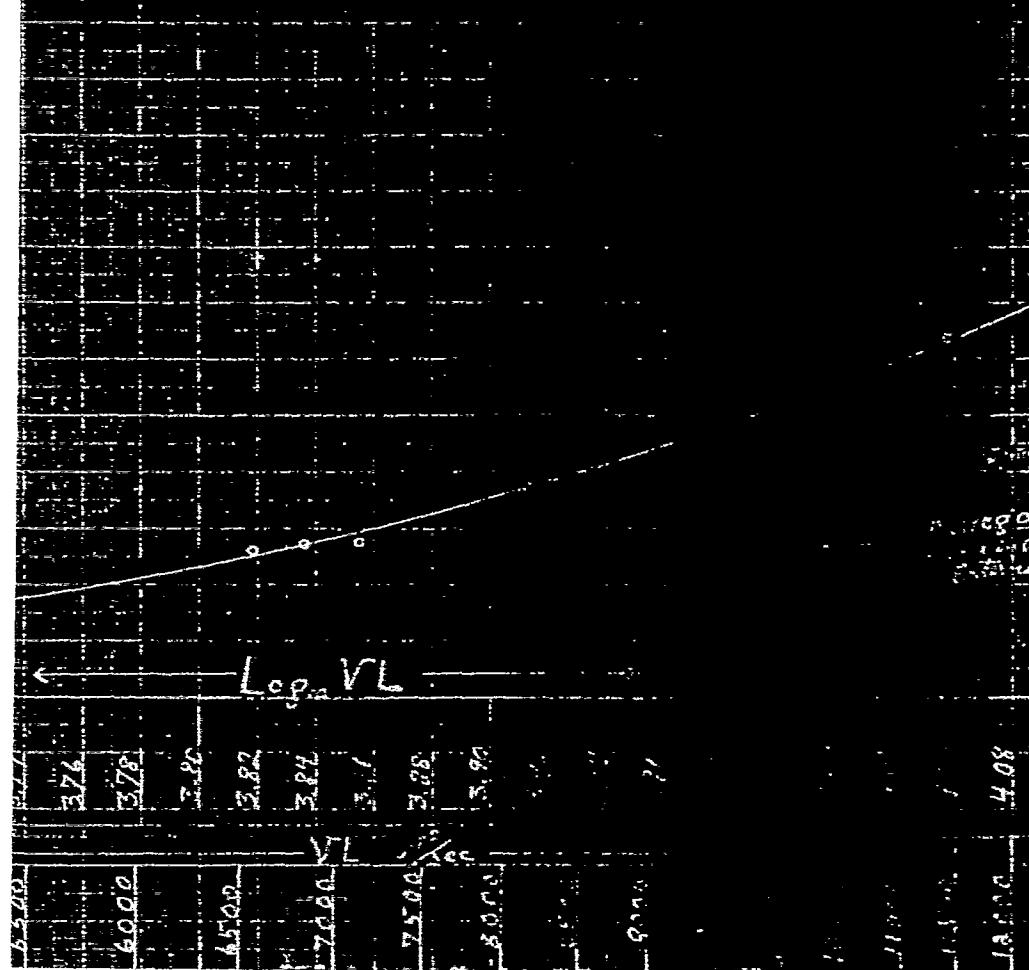
Are Airship Hull  
U.S.

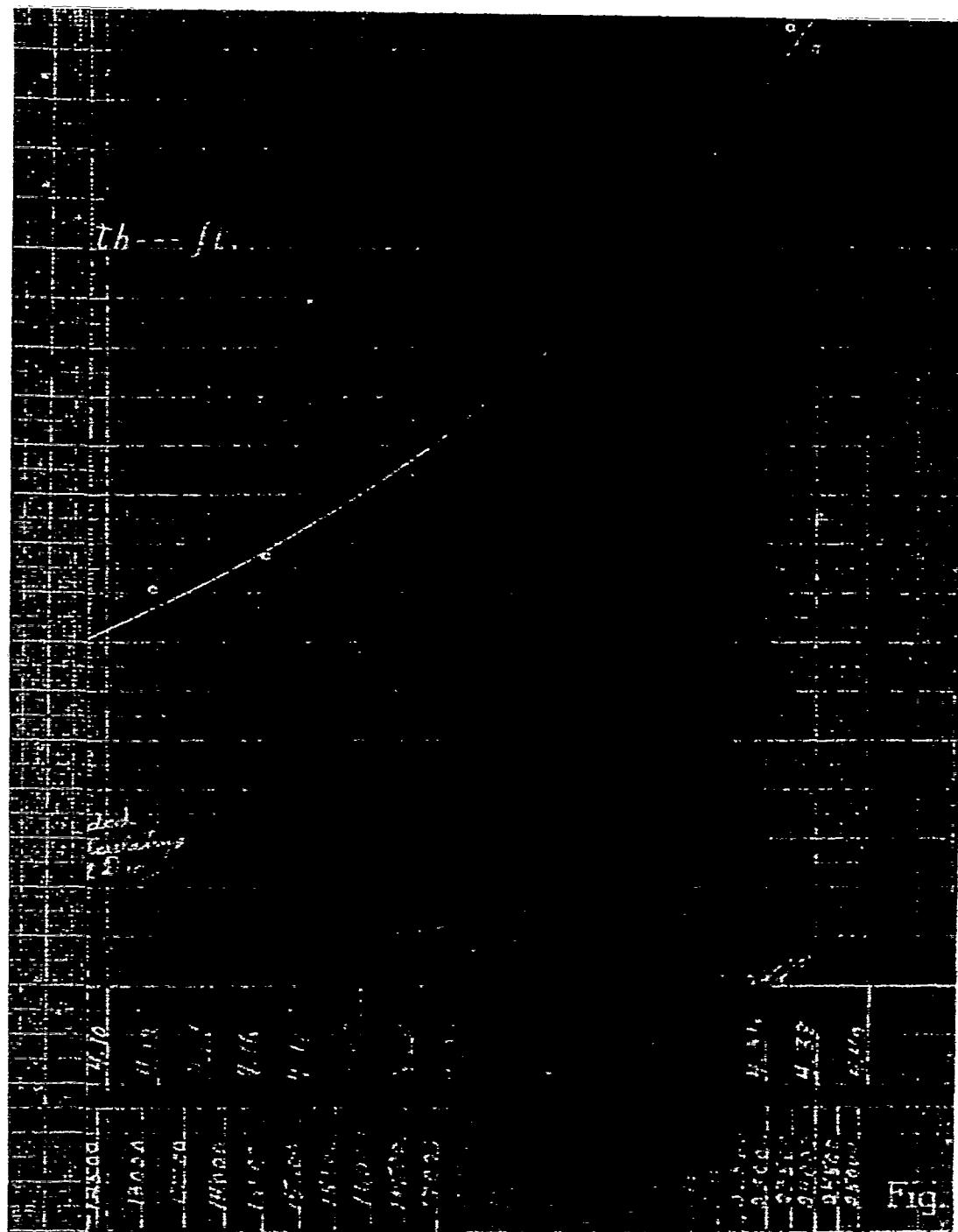
L

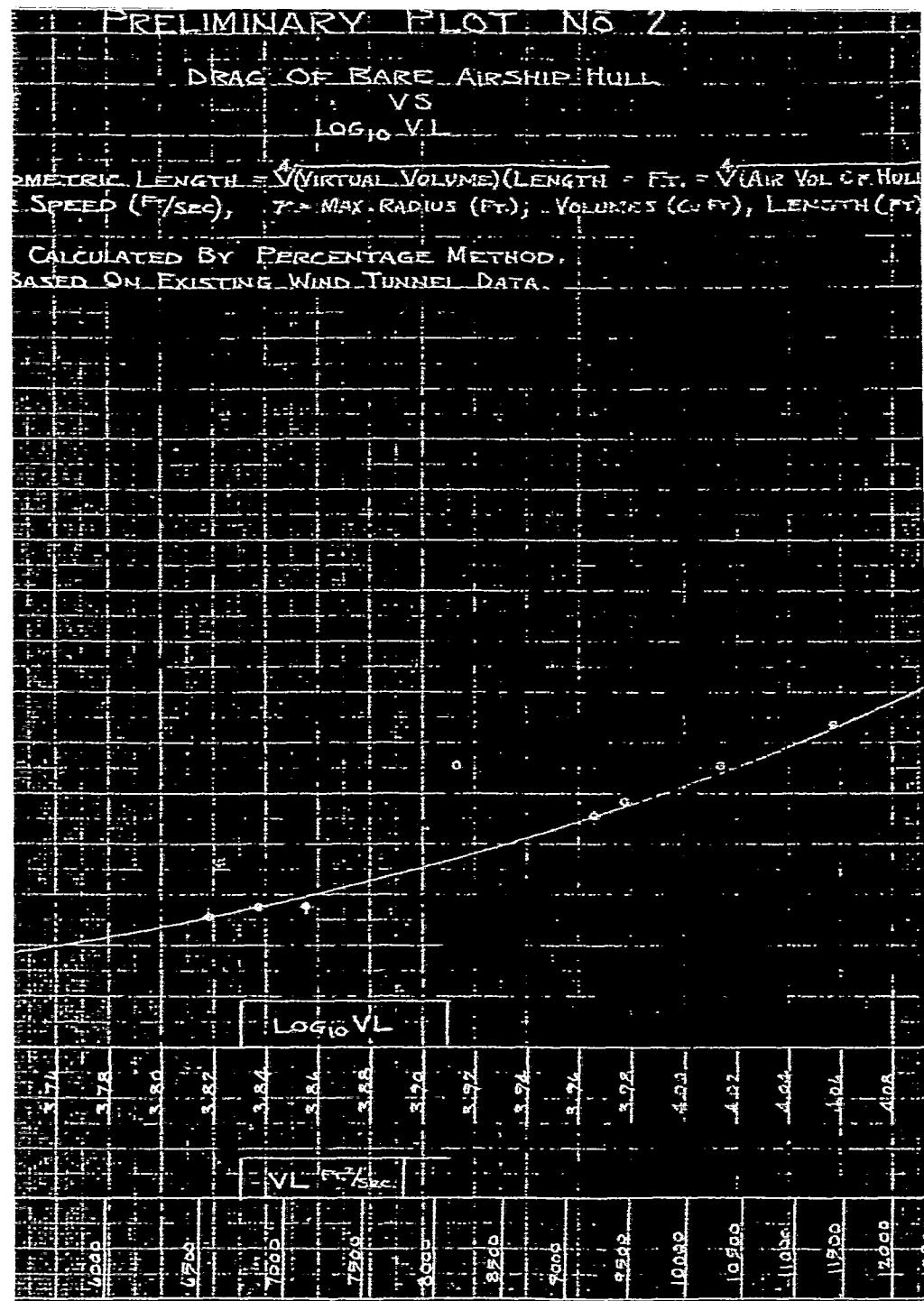
$$\text{Total Volume}^2 \times (\text{Length}) = \text{SL} = (\text{Volume})^2 / (\text{Radius})^2 \times (\text{Length})$$

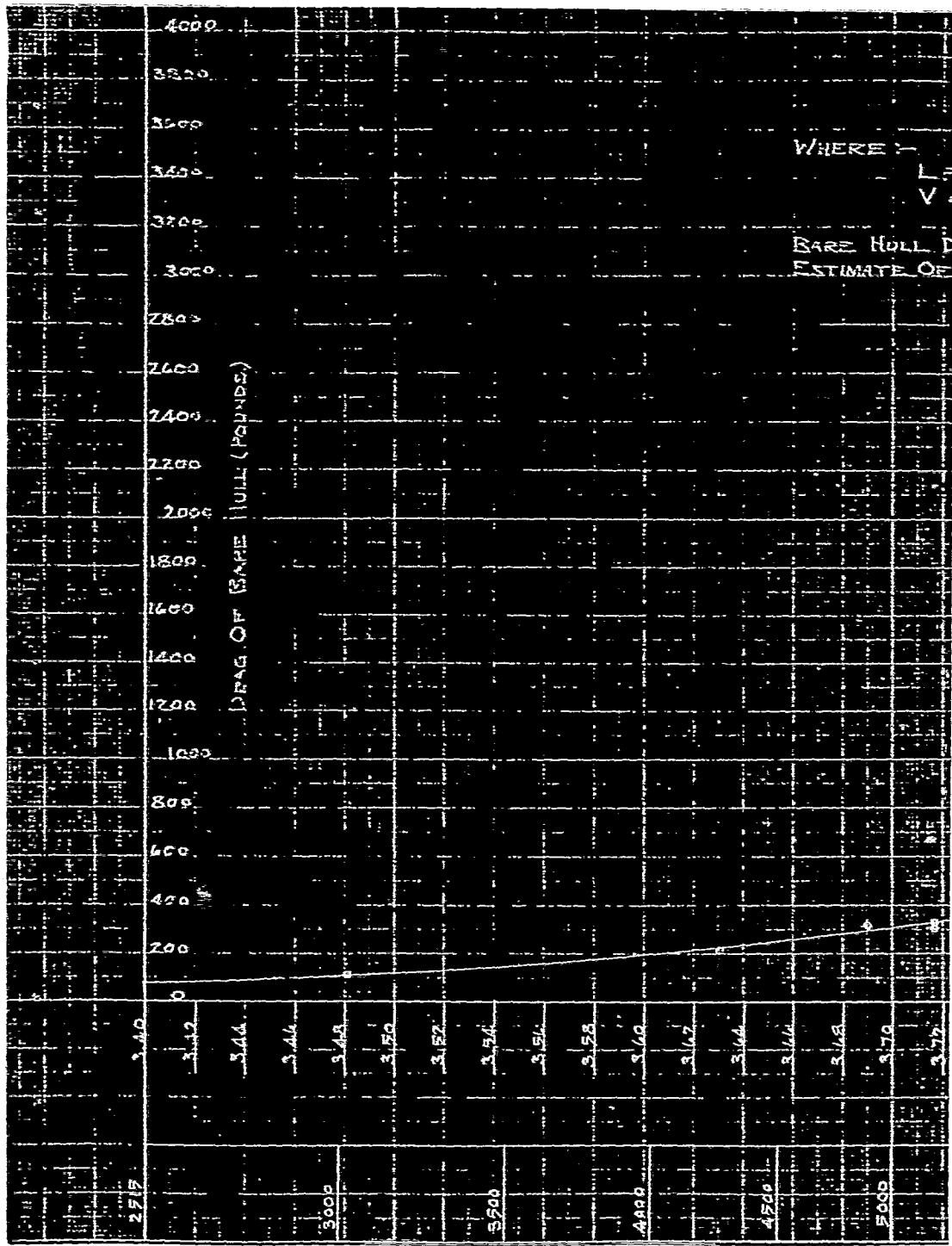
r = max. radius ft.      Volume = cu. ft.      Length = ft.

Difference between the calculated Estimated Length and the Actual Length obtained from the Log.







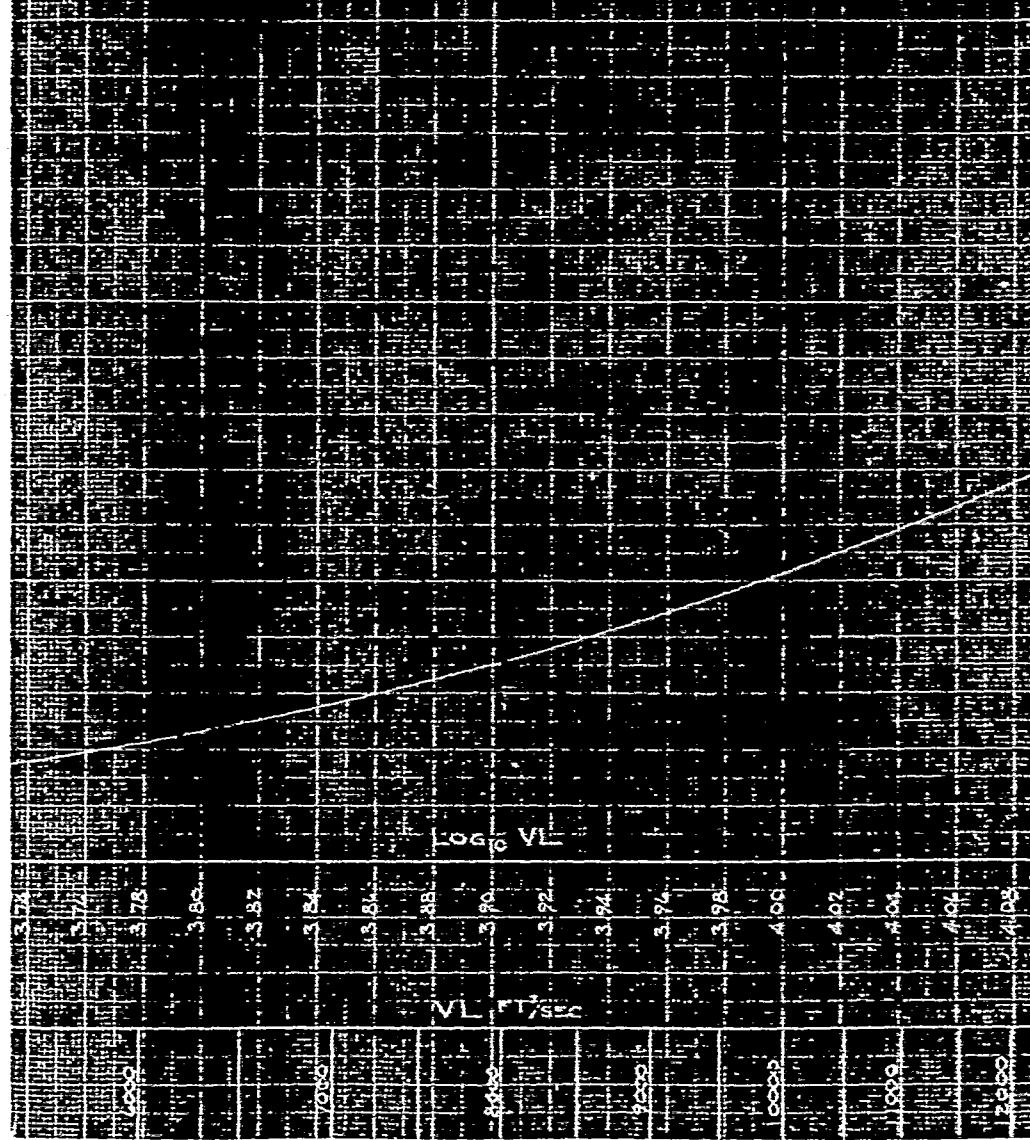


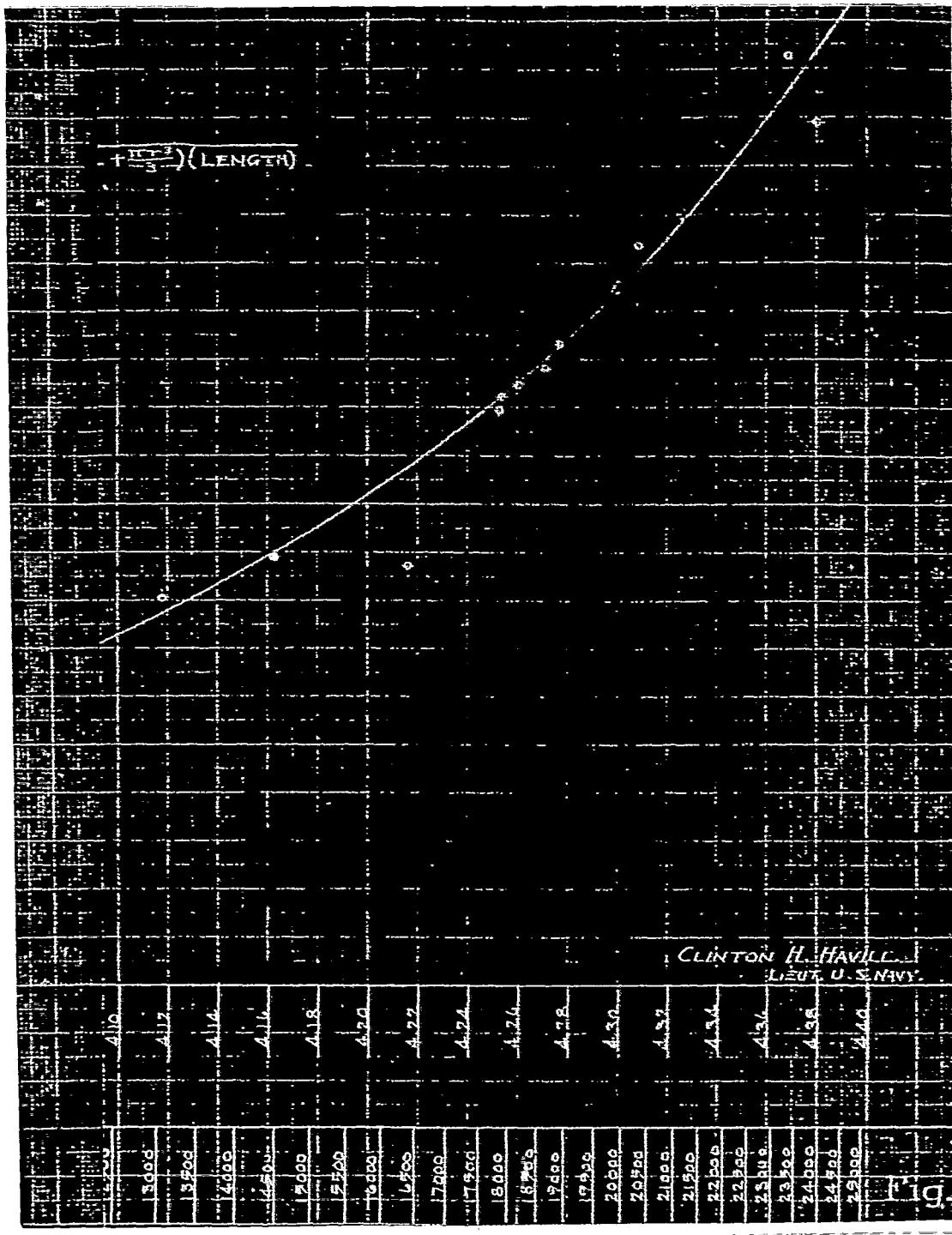
DRAG OF BARE AIRSHIP HULL

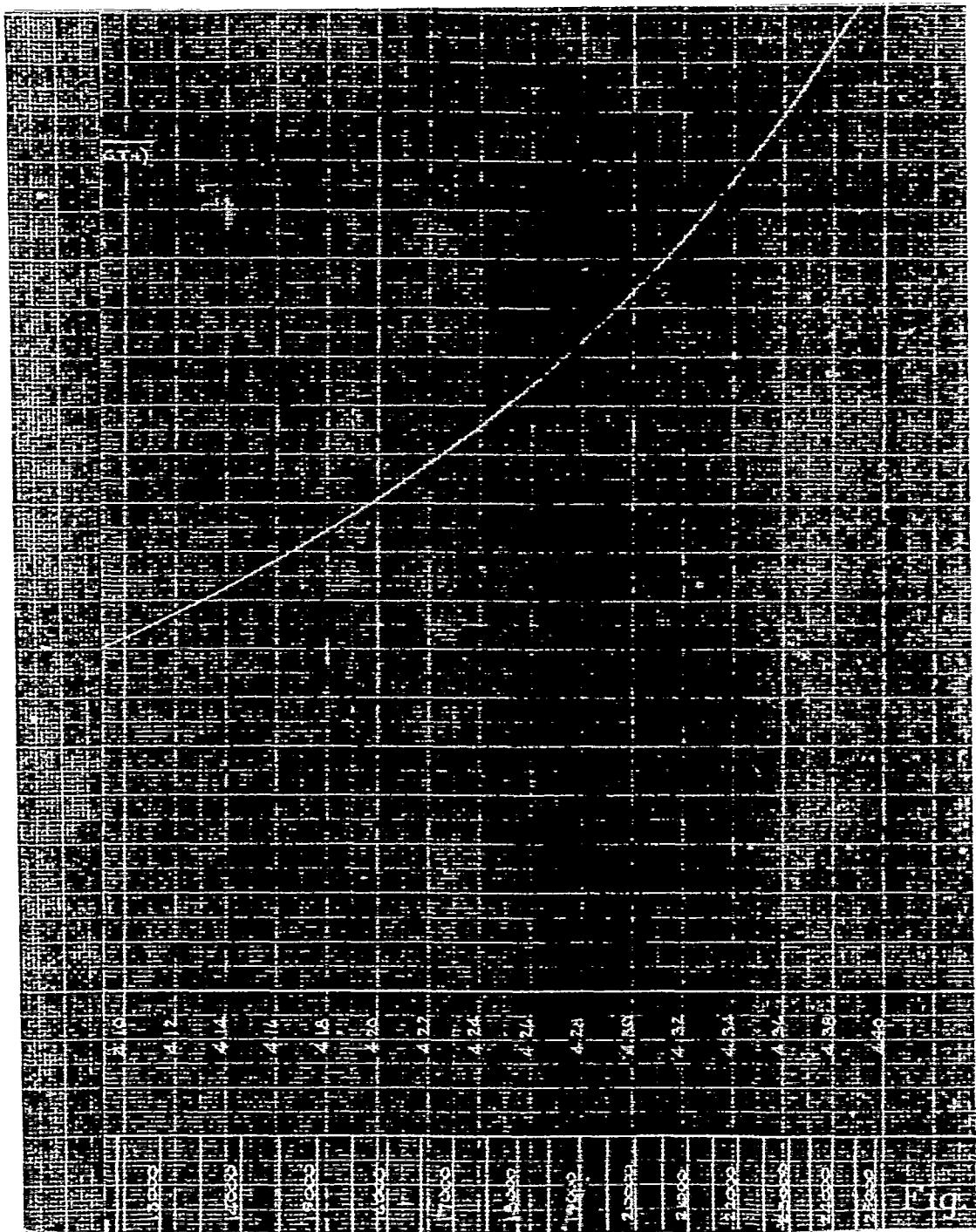
VS  
LOG<sub>10</sub> VL

GEOMETRIC LENGTH =  $\sqrt{V(VIRTUAL VOLUME)(LENGTH)} = \text{FT} = \sqrt{(\text{AIR VOL OF SHIP})^2 \times \text{LEN}}$   
 & SPEED (FT/SEC),  $r$  = HSA RADIUS (FT), VOLUMES (CU FT), LENGTH (FT).

Preliminary Plots 1 & 2







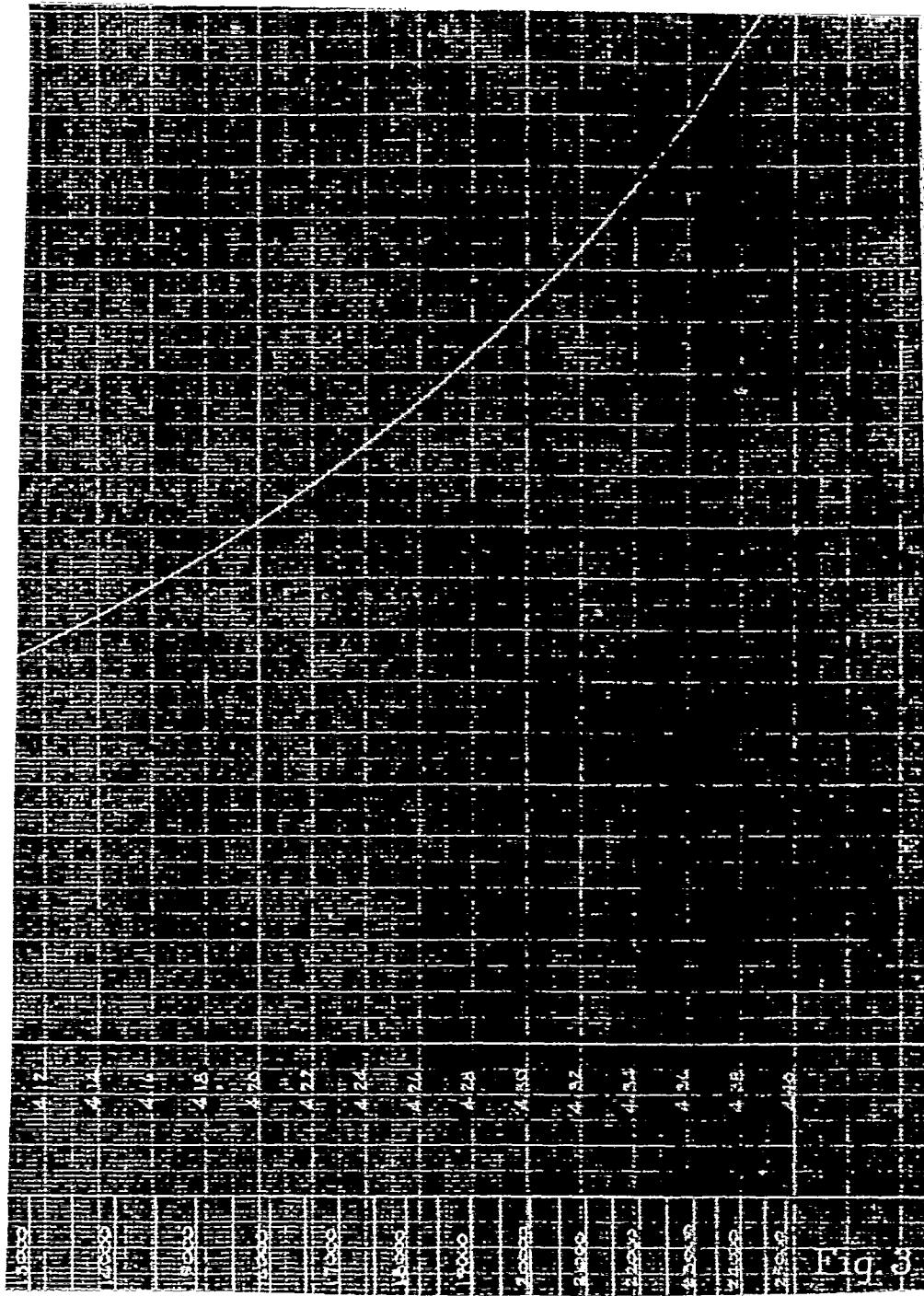
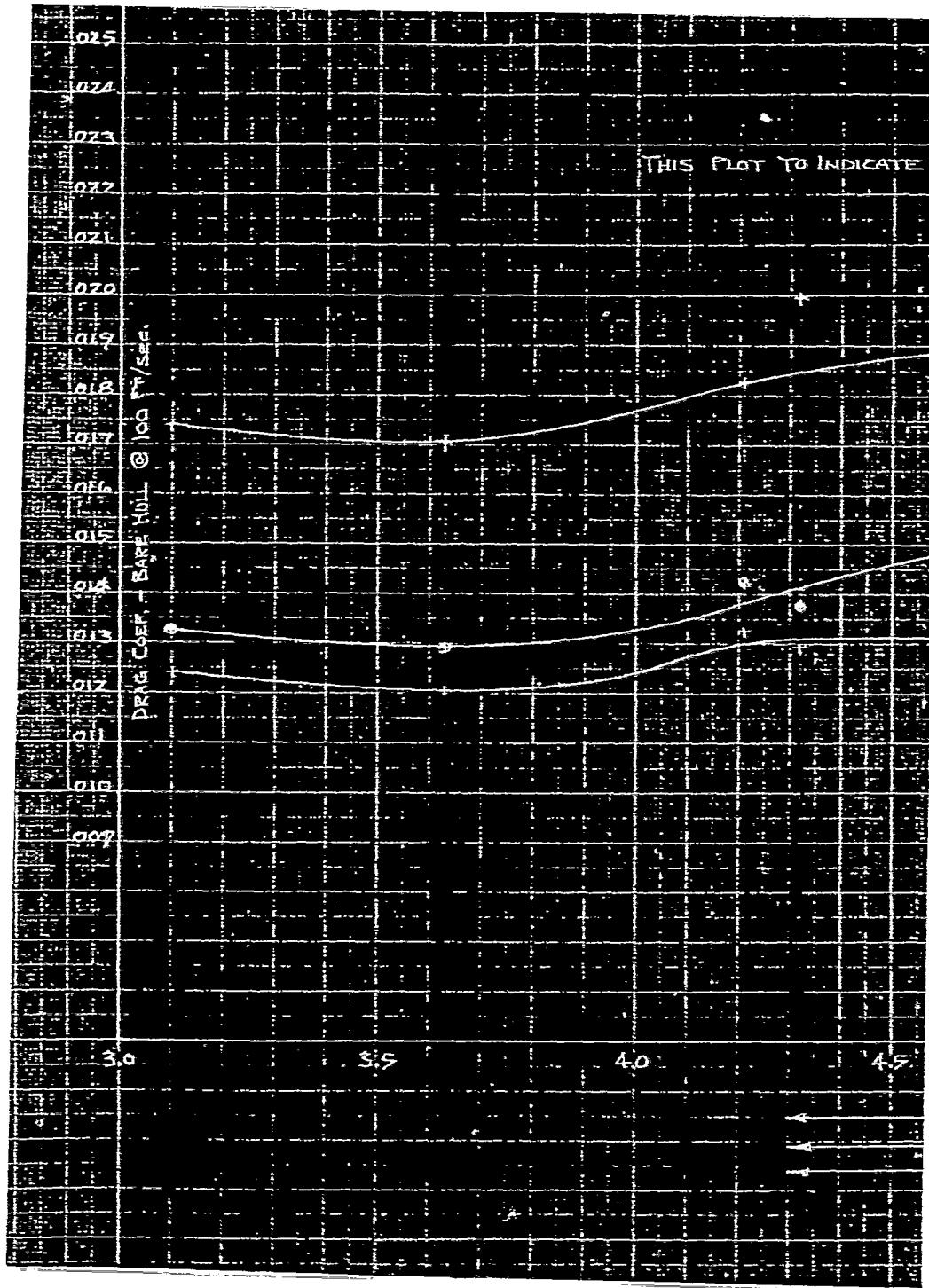


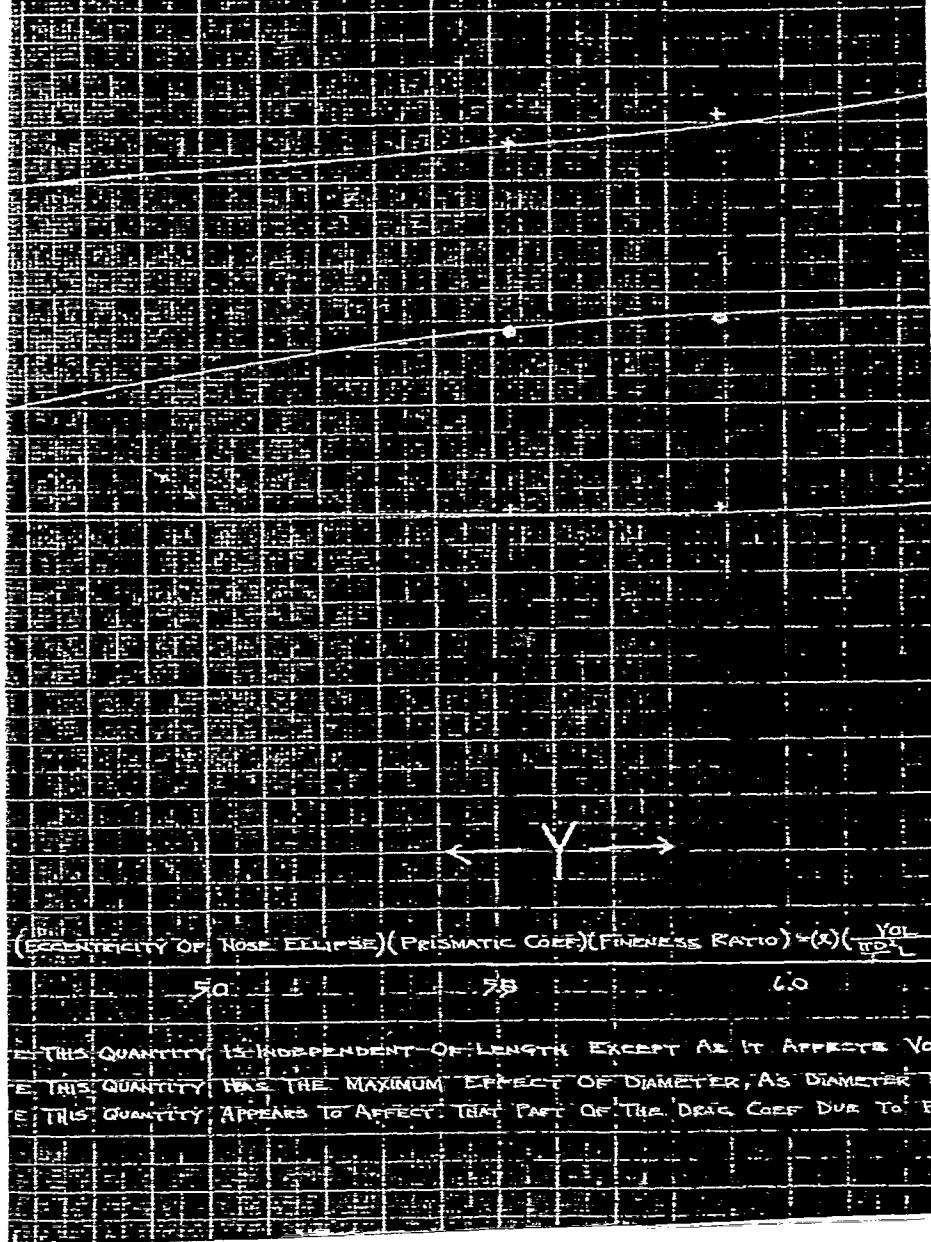
Fig. 3

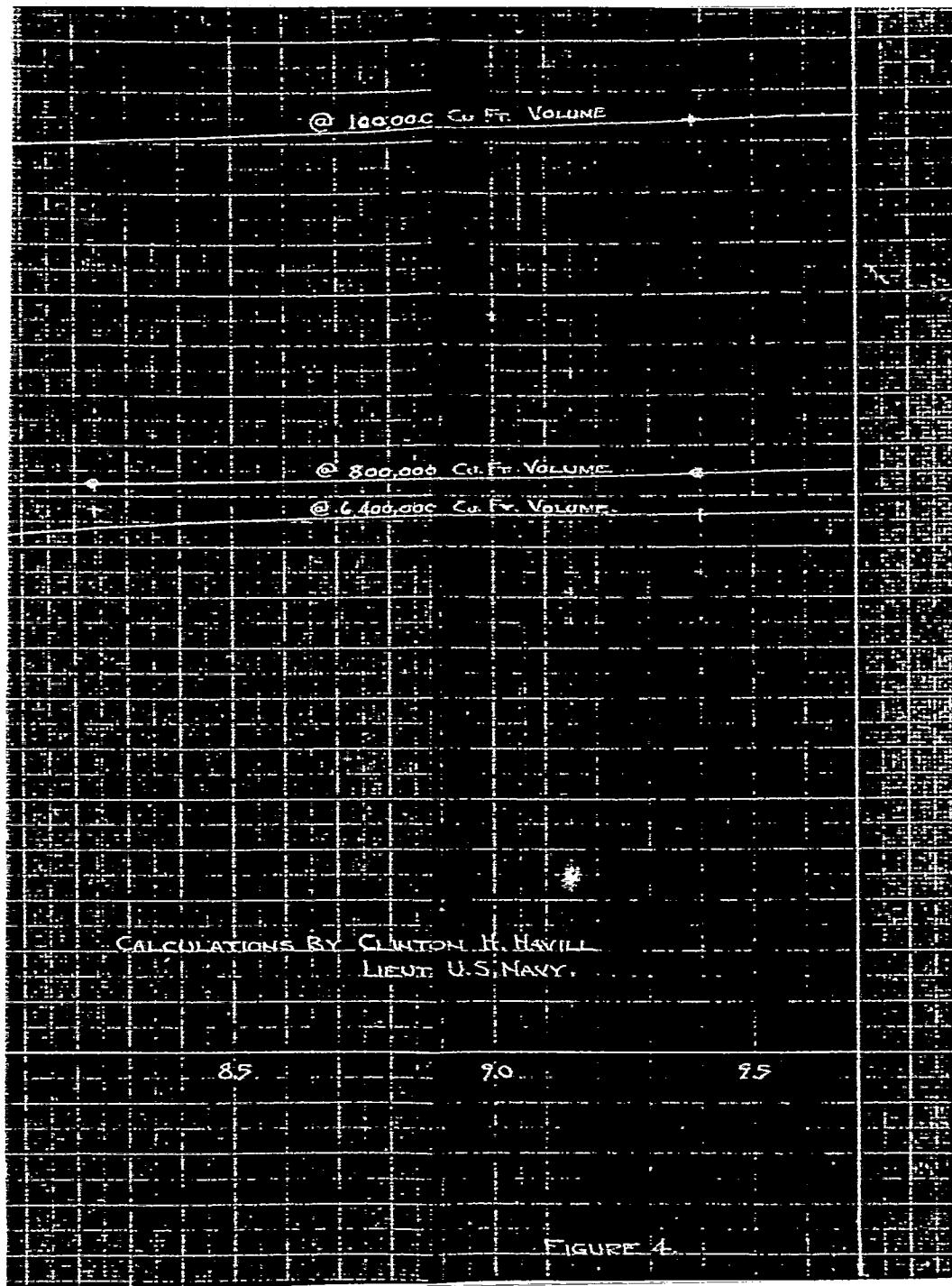


PRELIMINARY PLOT NO. 4

D.G. COEF. OF BARE HULL VS - (ECCENTRICITY OF NOSE ELLIPSE)

RELATION BETWEEN DRAG COEF., DIAMETER EFFECT, WITH VOLUME





IPSE) (PRISMATIC COEF.) (FINENESS RATIO)

WITH VELOCITY CONSTANT @ 100. FT/SEC.

$$D \left( \frac{L}{D} \right) = \left( 2 \right) \left( \frac{\Delta V_0 L}{\pi D^3} \right)$$

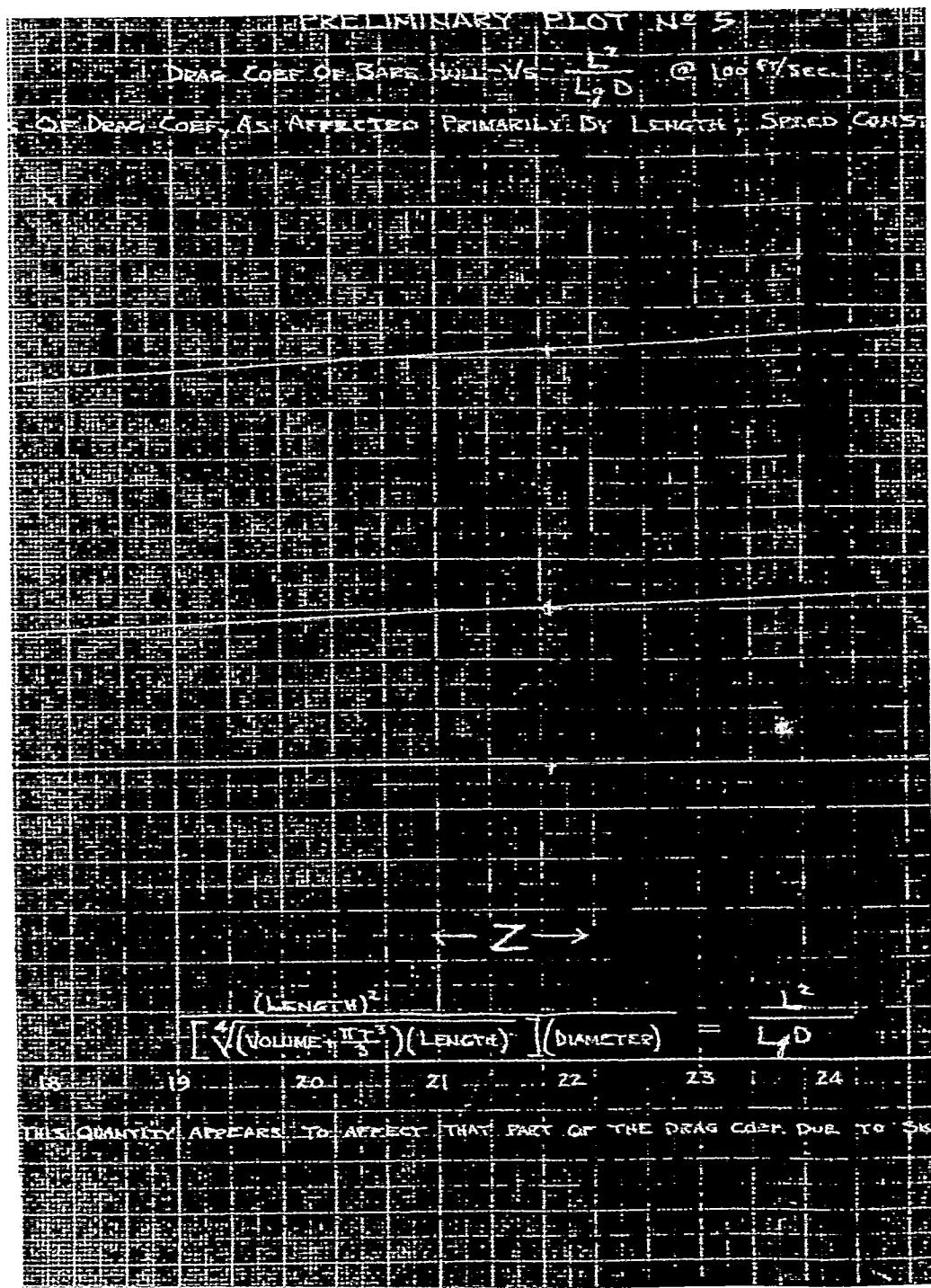
6.5

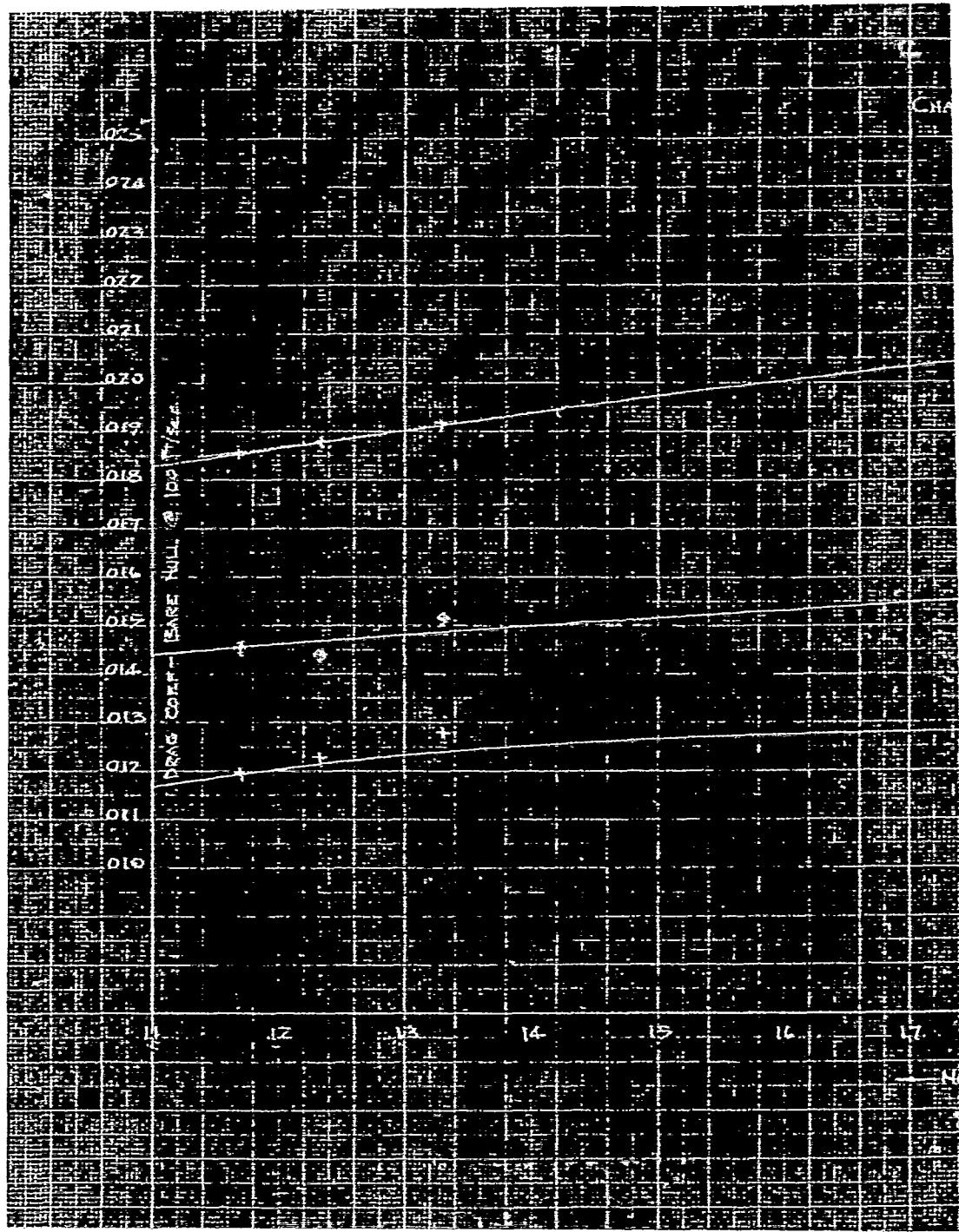
7.0

7.5

LINE

INTERES AS THE THIRD POWER.  
PRESSURE DIFFERENCE,





CALCULATIONS							
25	26	27	28	29	30	31	32
INERTION							

@ 100,000 Cu. Ft. Volume

@ 300,000 Cu. Ft. Volume

@ 6,450,000 Cu. Ft. Volume

BY CLINTON H. HAWK  
LIEUT. U. S. NAVY.

33 34 35 36 37 38 39

FIGURE 51

Part Of Wind Tunnel  
Isometric Drawing

Part Of Wind Tunnel (No)

NOTES -

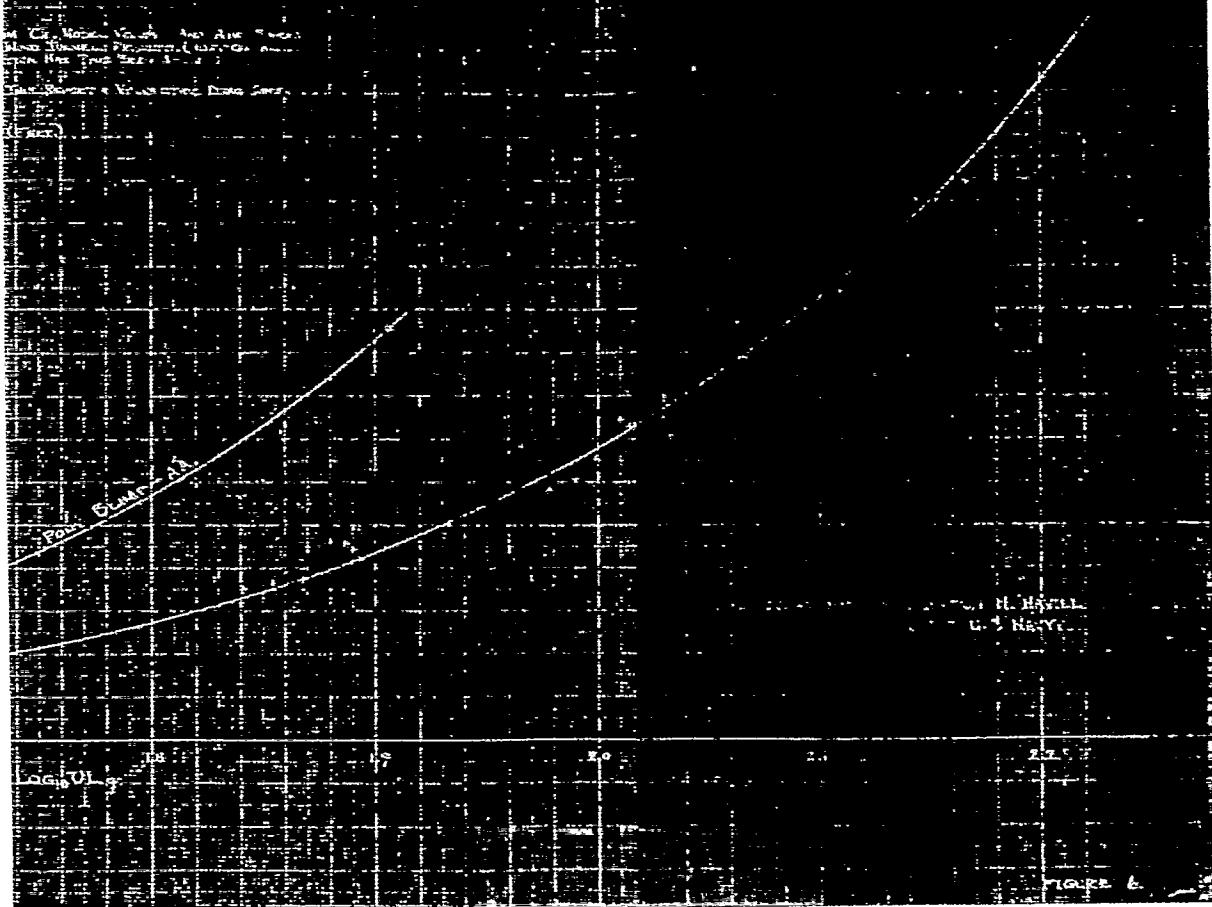
- DRAG =  $C_D \cdot \frac{1}{2} \rho V^2 A$  (LBS) As Reported  
 $C_D = 0.025$  (LBS)  
C - Constant  
D - Drag Coeff. - Drag Coeff. of Body as Used  
V - Wind Speed - Wind Tunnel (Ft/sec)  
L - Drag Coeff. of Body - (Ft/sec)  
W - Weight of Body - (Ft/sec)  
R - Rolling Resistance Coefficient - (Ft/sec)  
H - Height of Wheel - (Ft/sec)

NOTE - Due To Large Wind Tunnel Ratio Of 3.5 L/H, An  
Increase In Cx Will Be An Increase Of Df And  
This Due Increases Wind Resistance.

## RESULTS ON THE SEVENTEEN IN THE TEST.

15 May 2024

Mr. Charles V. Smith, 200 Ave. F.  
Brentwood, New York, (Long Island),  
open Sat. Evenings, 4-6 P.M.



E. WILSON HULL

LITERATURE, CONTOUR.

DEFINITIONS & SYMBOLS FOR THIS DIAGRAM:

- C = DRAG COEF OF BASE HULL (10 DIMENSIONS)
- C<sub>1</sub> = 1.0000
- D = DRAG OF BASE HULL (LB)
- D<sub>1</sub> = DRAG OF HULL (LB/FP)
- V = AIR SPEED. IN SEC.
- Y = LENGTH OF HULL (FT) OR (SKEW LENGTH)

Y = AN EMPIRICAL TERM WHICH PRIMARILY DETERMINES A FUNCTION - THAT PART OF THE DRAG COEF DUE TO PRESSURE DIFFERENCE.  
Y = NO. DIMENSIONS  
Y = GEOMETRICITY OF NOSE CYLINDRICAL COEF (FINENESS RATIO).

$$Y = \left( \frac{C}{C_1} \right)^{1/5}$$

$$Y = C \left( \frac{V^2}{D_1} \right)$$

WHERE

- C = DRAG COEF
- V = SPEED (LB/FP)
- Y = ELLIPTICITY OF NOSE ELLIPSE.

$$L = \frac{V^2}{D_1}$$

WHERE  
L = DISTANCE ALONG AXLE OF SHIP, FROM NOSE TO FIRST POINT  
OF NOSE DIAM.

$$Y = NOSE RADIUS = \frac{L}{2}$$

$$\text{CYLINDRICAL COEF} = \frac{V^2}{D_1}$$

$$\text{FINENESS RATIO} = \frac{Y}{L}$$

- C = AN EMPIRICAL TERM WHICH PRIMARILY DETERMINES A FUNCTION - THAT PART OF THE DRAG COEF DUE TO SKIN FRICTION.  
Y = NO. DIMENSIONS

$$C = \frac{1}{L^2}$$

$$C = \frac{(\text{GEOMETRIC LENGTH})}{(\text{FINENESS RATIO})}$$

$$C = \left( \frac{L}{Y} \right) \left( \frac{C}{C_1} \right)^{1/5}$$

WHERE

- L = LENGTH OF HULL (FT)
- L = TERM OF LINEAR DIMENSIONS USED TO COMPARE SHIPS AT THE  
SAME DRY - DEFINED IN TEXT AS GEOMETRIC LENGTH.

$$L = \frac{\text{VOL.}}{\text{AV. VOL.}}$$

$$L = \frac{V^2}{D_1}$$

WHERE VOL = VOL OF SHIP  $\frac{L^3}{12}$  (CB FT)

$$L = \frac{V^2}{D_1}$$

$$L = \frac{V^2}{D_1} [C + F (\text{SEE FORM})]$$

$$L = \frac{V^2}{D_1}$$

THIS DIAGRAM FOR STANDARD VALUE OF  $\frac{C}{C_1}$

DIRECTIONS FOR USE - CALCULATE "Y & L" AND DO THEM. ENTER THE LEFT HAND SCALE WITH THE VALUE OF LENGTH (Y & L) AND FOLLOW THEM HORIZONTALLY TO SCALE OF C/C<sub>1</sub>. DO C/P THEN, FOLLOW ACROSS THE DRAIK, INTERPOLATING THE SLOPE BETWEEN THE ADJACENT SLOPE LINES. PICK OFF THE DRAG COEF'S AT VOLUMES OF 100,000 - 800,000 & 6,000,000 CF. PT. THESE DRAG COEF'S, ARE FOR THE VOLUMES GIVEN AT 100 MPH AIR SPEED. FOR INTERPOLATION FOR VOLUMES OTHER THAN THOSE GIVEN, PROCEED AS FOLLOWS: WITH THE THREE VALUES OF DRAG COEF, AS PICKED OFF FROM THE DIAGRAM CALLED "COURT CURVE". PLOT THE LOG<sub>10</sub> OF THESE THREE VALUES AGAINST THE LOG<sub>10</sub> OF LENGTH (L), WHERE LENGTH IS THE LENGTH AT VOLUMES OF 100,000, 800,000 & 6,000,000 CF. PT. FOR REDUCTION OR EXPANSION OF LENGTH, USE FORMULA  $L' = L \cdot 10^{(Y-1)}$ . THE CURVE OF LOG<sub>10</sub> DRAG COEF (LOG<sub>10</sub> OF DRAG COEF) WITH EACH TYPE OF SHIP PASS A SMOOTH CURVE THROUGH THE THREE POINTS ESTABLISHED (USE REASONABLY SMALL ON SCALE) AND PICK OFF THE VALUE OF DRAG COEF, THAT CORRESPONDS TO A VOL UP 100 TIMES LENGTH UP THE PARTICULAR SHIP. FOR FURTHER INFORMATION SEE PART II OF TEXT. SEE EXAMPLE FOR ILLUSTRATING USE OF THIS DIAGRAM IN PART II OF TEXT.

CALCULATIONS BY Clinton H. Harrell  
TEST U.S.NAVY

FIGURE 7.

DIAGRAM SHOWING THE CHANGE OF DRAG COEFFICIENT  
WITH VOLUME, SPEED CONSTANT @ 100  
FROM MODEL TO FULL SIZE - FOR AIRSHIP HULLS WITH CONST.

FOR HULLS WITH CONTINUOUS CURVATURE CONTOUR, FINENESS RATIOS 2.41 TO 7.25, CRITICAL COEF. 587.5<sup>1/2</sup>,  
ECCENTRICITY OF NOSE ELLIPS. 1.732 TO 1.778, AND DISTANCE FROM NOSE TO MAXIMUM ORDINATE 30% TO 47.33% LENGTH

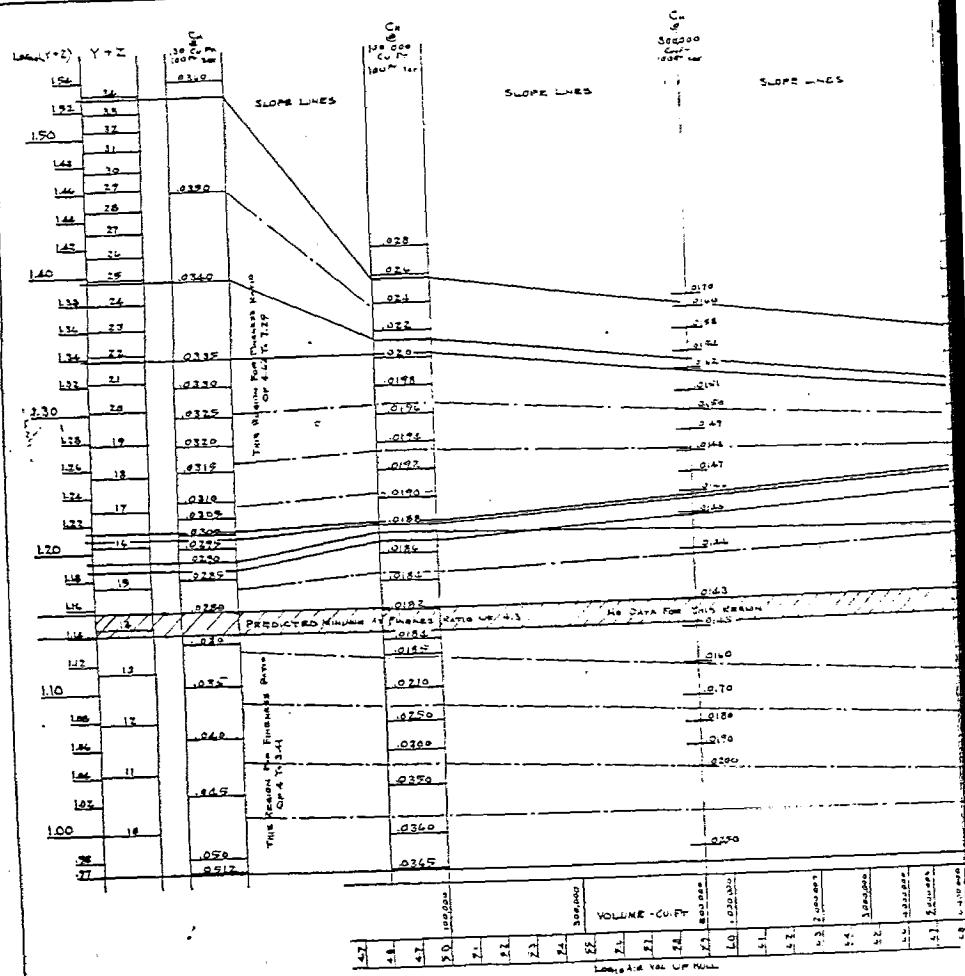
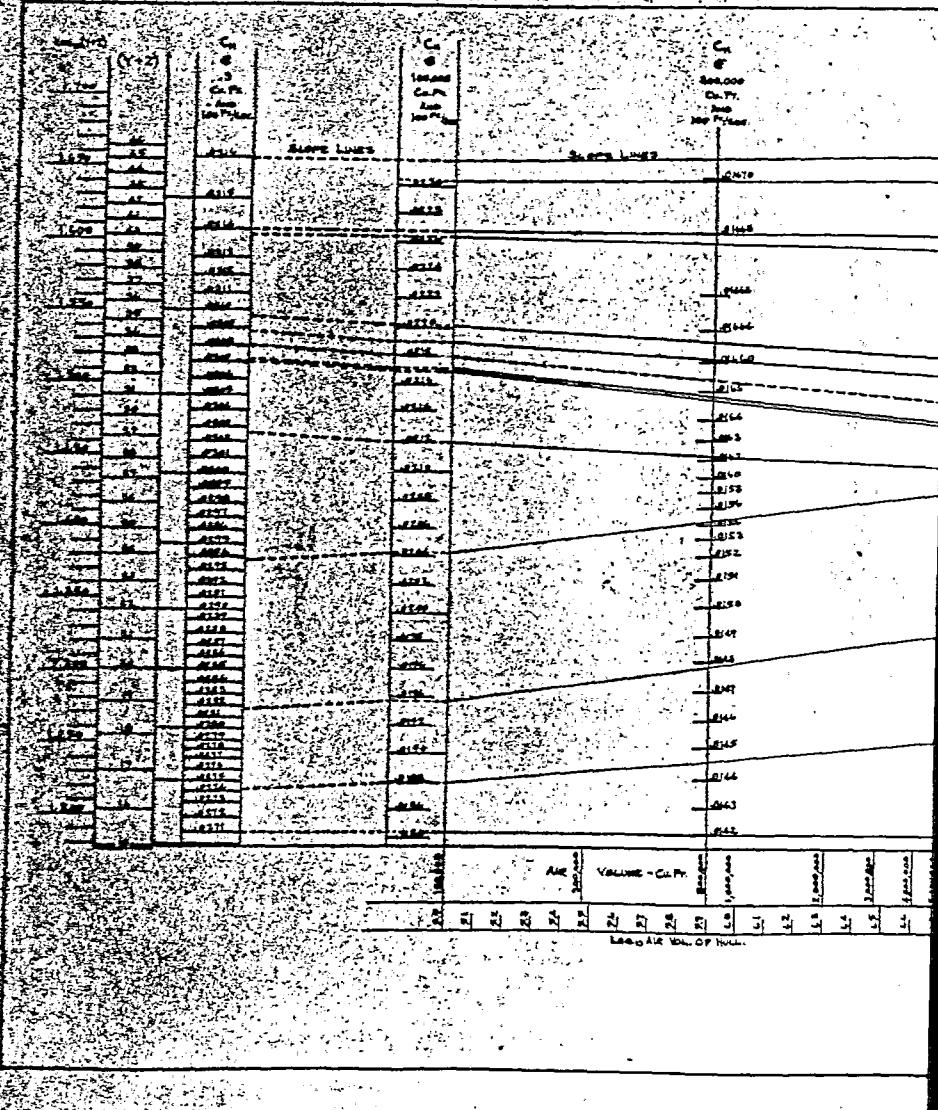


DIAGRAM SHOWING THE CHANGE OF DRAG COEFFICIENT  
WITH VOLUME, SPEED CONSTANT  
FROM MODEL TO FULL SIZE - FOR AIRSHIP HULLS WITH

NOTES ON THE DATA FROM WHICH THIS WAS DERIVED - THE HULLS WITH PARALLEL SECTIONS EQUAL TO NOT LESS THAN 1/4 OF THE DIAHMETRE RATIO FROM 45% TO 100% CYLINDRICAL COEFFICIENT FROM .165 TO .516, ECCENTRICITY OF NOSE ELLIPSE FROM .532 TO .950, DISTANCE FROM NOSE TO FIRST MAXIMUM CHORDS FROM 14.5% TO 30.84% OF THE LENGTH.



BARE AIRSHIP HULLS

T/SEC.

16. SECTIONS.

PRINCIPAL TYPE OF HULL WHICH IS CHARACTERISTIC TO THAT PART OF THE SCALE. (COMPLETE DATA FROM WHICH THIS DIAGRAM WAS PLOTTED, IS GIVEN IN THE TEXT.)

ITEM 8 TEXT L211 BULLETS NUMBERED ZEPPELIN.

ITEM 11 TEXT L210 & L112 BULLETS NUMBERED ZEPPELIN.

U.S NAVY "C" WITH 7 DIA. PARALLEL SECTION.

ITEM 17 TEXT L212-20 BULLETS NUMBERED ZEPPELIN.

U.S NAVY "C" WITH 4 DIA. PARALLEL SECTION.

ITEM 18-19-20 & L212 (PART I & PART II OF TEXT)

SHIPS SHREWDORN (HAGA) AND ZEPPELIN.

U.S NAVY "C" WITH 3 DIA. PARALLEL SECTION.

U.S NAVY "C" WITH 2 DIA. PARALLEL SECTION.

EXAMPLE ILLUSTRATED IN TEXT.

ITEMS 18-19-20 & L212 (PART I & PART II OF TEXT)

SHIPS SHREWDORN (HAGA) AND ZEPPELIN.

U.S NAVY "C" WITH 1 DIA. PARALLEL SECTION.

U.S NAVY "C" WITH 1/2 DIA. PARALLEL SECTION.

U.S NAVY "C" WITH 1/4 DIA. PARALLEL SECTION.

DEFINITIONS & SYMBOLS FOR THIS DIAGRAM.

$C_d$  = DRAG COEF. OF BARE HULL (NO DIMENSIONS)

$C_d = \frac{1}{(C_d)^{1/2}}$

$R_d$  = DRAG OF BARE HULL, (LB.)

$V_{el}$  = AIR VOL. OF HULL, (CUBIC FT.)

$V$  = AIR SPEED, (FT./SEC.)

$\rho$  = DENSITY OF AIR, (LB./CU. FT.) OR (SLUG/CU. M.)

$Y$  = AN EMPIRICAL TERM WHICH PRIMARILY DETERMINES A PROPORTION - THAT PART OF THE DRAG COEF. DUE TO PRESSURE DIFFERENCE.

$Y$  = (NO DIMENSIONS)

$Y = (\text{ECCENTRICITY OF HULL SHAPE}) \times (\text{CYLINDRICAL COEF.}) \times (\text{PROGRESSION RATIO})$

$Y = (A)(\frac{V}{V_{el}})(B)$

$Y = (A)(\frac{V}{V_{el}})(B)$

WHERE:

$A = \text{HULL DIAM. (FEET)}$

$V_{el} = \text{VOLUME (CUBIC FT.)}$

$B = \text{ECCENTRICITY OF HULL ELLIPSE}$

$C = \sqrt{\frac{V_{el}}{V}}$

WHERE:

$X = \text{DISTANCE ALONG AXIS OF SHIP, FROM HULL TO POINT (W) ON HULL DIAM.}$

$T = \text{HULL DIAM. = DIAM.}$

$\text{CYLINDRICAL COEF.} = \frac{1}{V_{el}}$

$\text{PROGRESSION RATIO} = \frac{1}{V_{el}}$

$Z$  = AN EMPIRICAL TERM WHICH PRIMARILY DETERMINES A PROPORTION - THAT PART OF THE DRAG COEF. DUE TO SKIN FRICTION.

$Z$  = (NO DIMENSIONS)

$Z = (\text{LENGTH}) / (\text{GEOMETRIC LENGTH}) \times (\text{FINENESS RATIO})$

$Z = (\frac{L}{L_g})(\frac{L}{L_g}) = \frac{L^2}{L_g^2} = \frac{L^2}{40}$

WHERE:  $L_g$  = LENGTH OF HULL (FT.)

$L_g$  = A TERM OF LINEAR DIMENSIONS USED TO COMPARE SHIPS AT THE SAME U.D.L. - DEFINED IN TEXT AS "GEOMETRIC LENGTH".

$L_g = \sqrt{V_{el} / L}$

$L_g = \sqrt{V_{el} / (L \times V_{el})} = (C/F)$

$L_g = \sqrt{V_{el} / (L \times V_{el})} = (C/F)$

$L_g = (C/F)$

THIS DIAGRAM FOR STANDARD VALUE OF  $\frac{C_d}{\rho}$ .

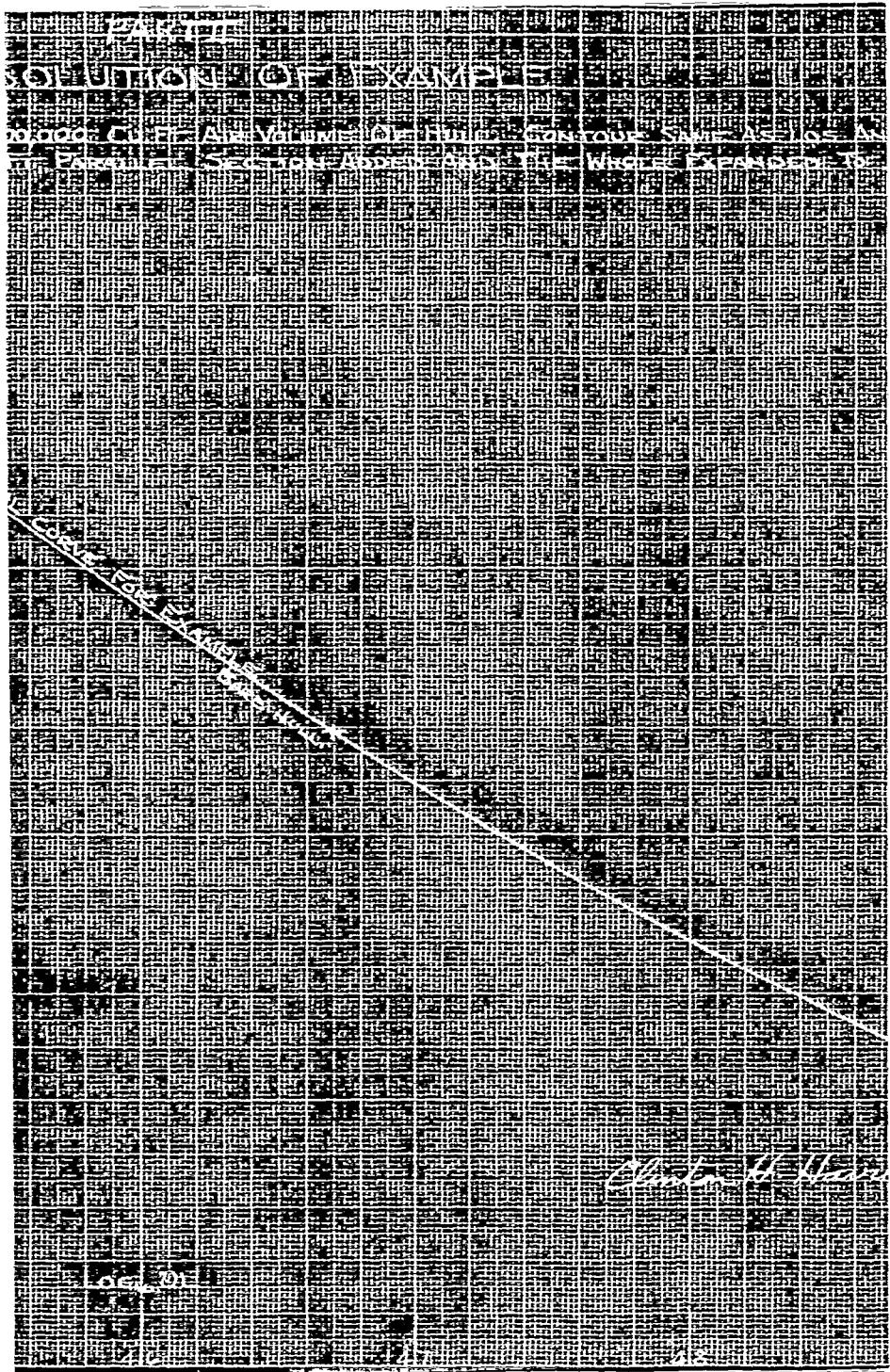
DIRECTIONS FOR USE:

CALCULATE "Y" & "Z" AND ADD THEM. ENTER THE LEFT HULL SCALE WITH THE VALUE OF  $L_{100}(Y+Z)$  AND FOLLOW THEREIN HORIZONTALLY TO SCALE OF  $C_d/(\rho)$ . FROM THEM FOLLOW ACROSS THE DIAGRAM, INTERPOLATING THE SUMS BETWEEN THE ADJACENT SLICE LINES. PICK OFF THE DRAG COEFS. AT VOLUMES OF 100,000 - 500,000 CUBIC FT. THESE DRAG COEFS. ARE FOR THE VOLUMES GIVEN AT 100' SEC. AIR SPEED. FOR INTERPOLATION FOR VOLUMES OTHER THAN THOSE GIVEN, PROCEED AS FOLLOWS. WITH THE THREE VALUES OF DRAG COEF. AS PICKED OFF FROM THE DIAGRAM, CALLED  $C_d(1)$ ,  $C_d(2)$ ,  $C_d(3)$ , PLOT THE LOGS OF THESE THREE VALUES AGAINST THE LOGS OF  $(L_{100}/100)$  (WHERE LENGTH IS THE LENGTH AT VOLUMES OF 100,000 - 500,000 CUBIC FT., FOR REDUCTION OR EXPANSION [LOGS OF LENGTH]). THE CURVE OF LOGS OF DRAG COEF. VS LOGS OF LENGTH DIFFERS WITH EACH TYPE OF SHIP. PASS A SMOOTH CURVE THROUGH THE THREE POINTS ESTABLISHED (USE PROBABLY SMALL DRAG SCALE) AND PICK OFF THE VALUE OF DRAG COEF. THAT CORRESPONDS TO A UL OF 100 TIMES LENGTH OF THE PARTICULAR SHIP. FOR FURTHER INFORMATION SEE PART II OF TEXT. SEE EXAMPLE FOR ILLUSTRATING USE OF THIS DIAGRAM IN PART II OF TEXT.

CALCULATIONS BY Clinton H. Havill  
Lieutenant Commander U.S. Navy

FIGURE 3.





LES  
000,000 CU. FT.

$\log_{10} C_H @ 100 \text{ ft/sec.} = 8.147 - 10$   
 $C_H = .01403 @ \{ \text{DESIGNED VOLUME OF } 5,000,000 \text{ CU. FT.} \}$  REQUIREMENT No 1.  
(AIR SPEED 100 FT/SEC.)

$\log_{10} C_H @ 120 \text{ FT/SEC.} = 8.132 - 10$   
 $C_H = .01355 @ \{ \text{DESIGNED VOLUME OF } 5,000,000 \text{ CU. FT.} \}$  REQUIREMENT No 2.  
(AIR SPEED 120 FT/SEC.)

Figure 9